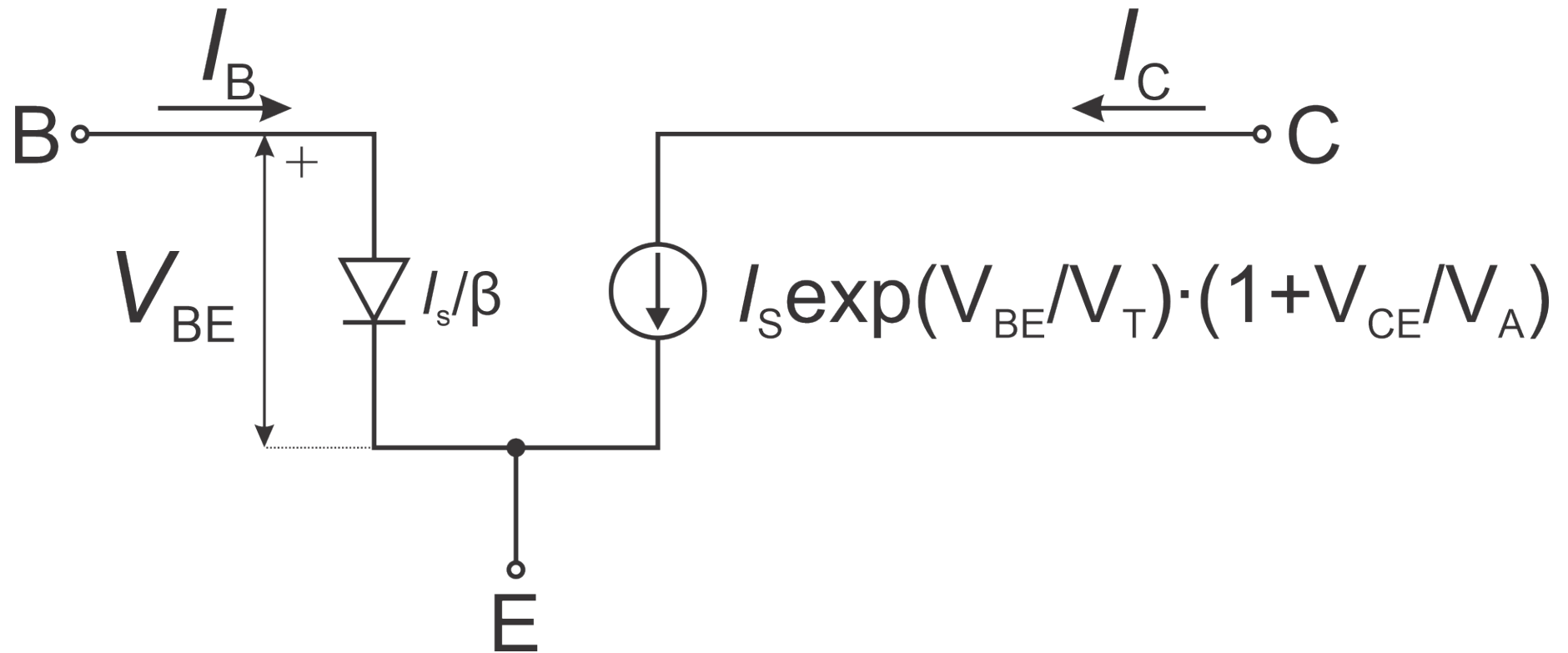


# Pojačavači sa bipolarnim tranzistorima

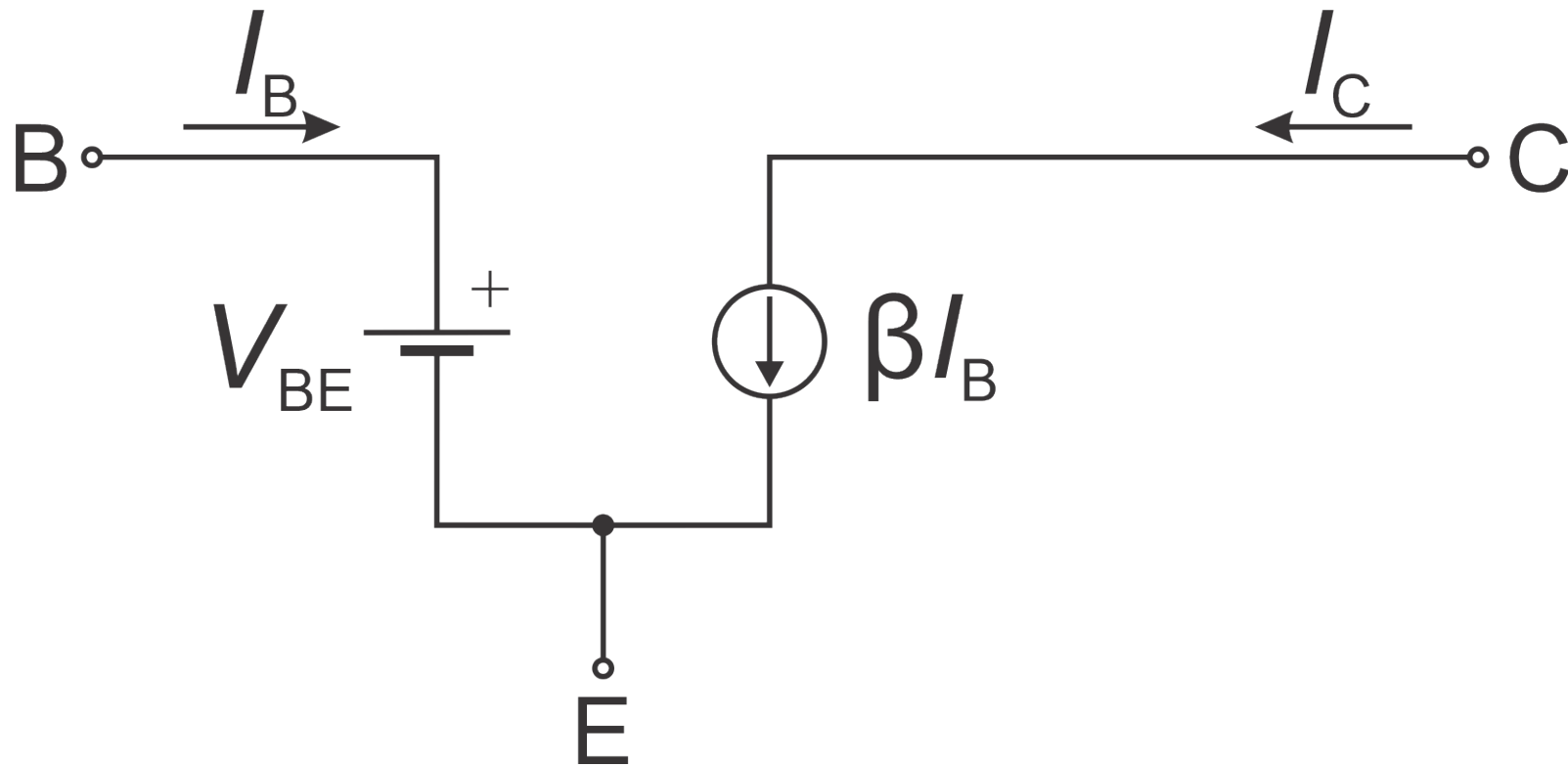
# Model za velike signale (polarizacija)

Parametri:  $I_S$ ,  $\beta$ ,  $V_A$



# Model za velike signale (linearizovani)

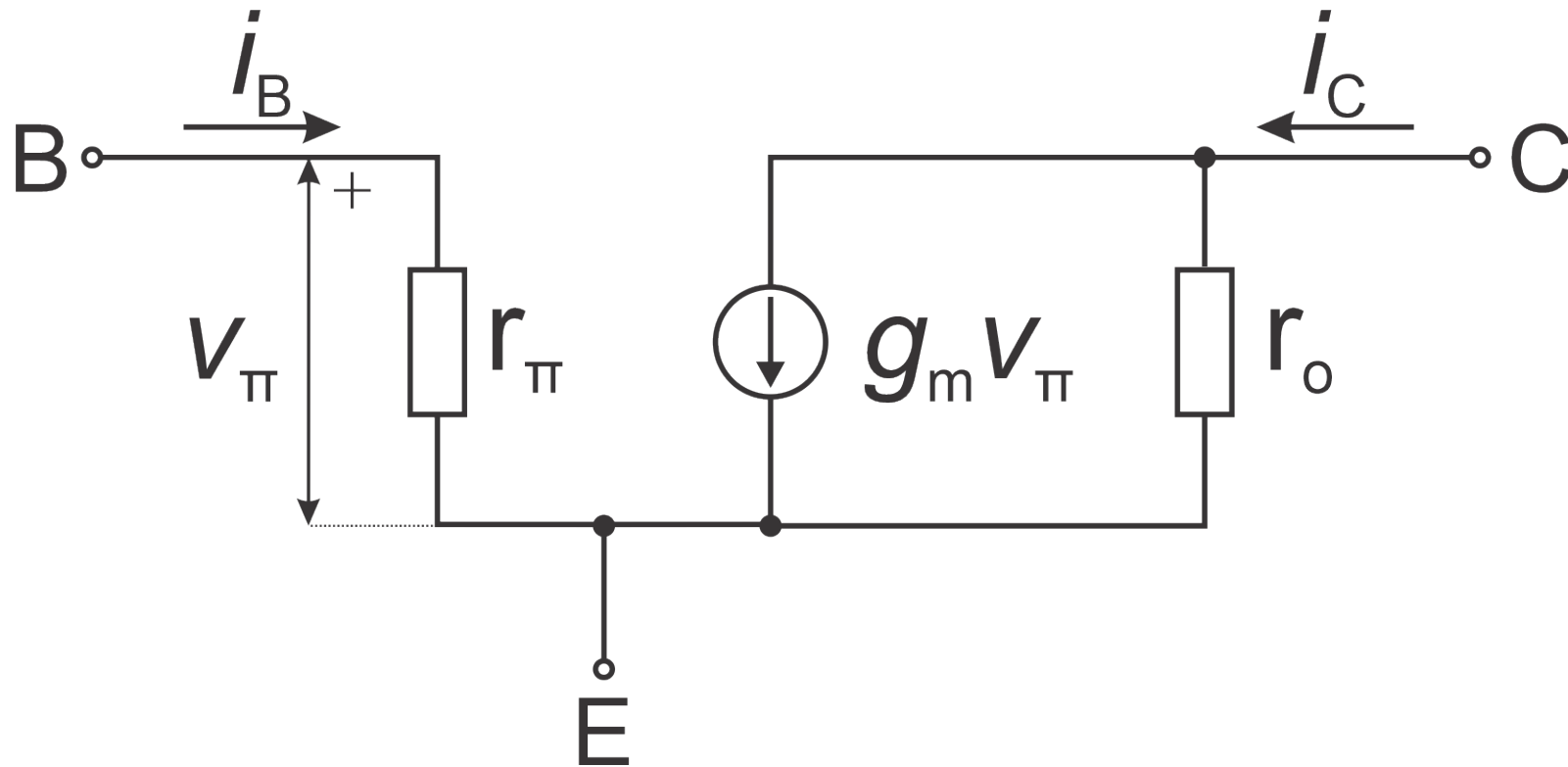
Parametri:  $\beta$ ,  $V_{BE}$



# Model za male signale

Parametri:  $g_m$ ,  $r_\pi$ ,  $r_o$

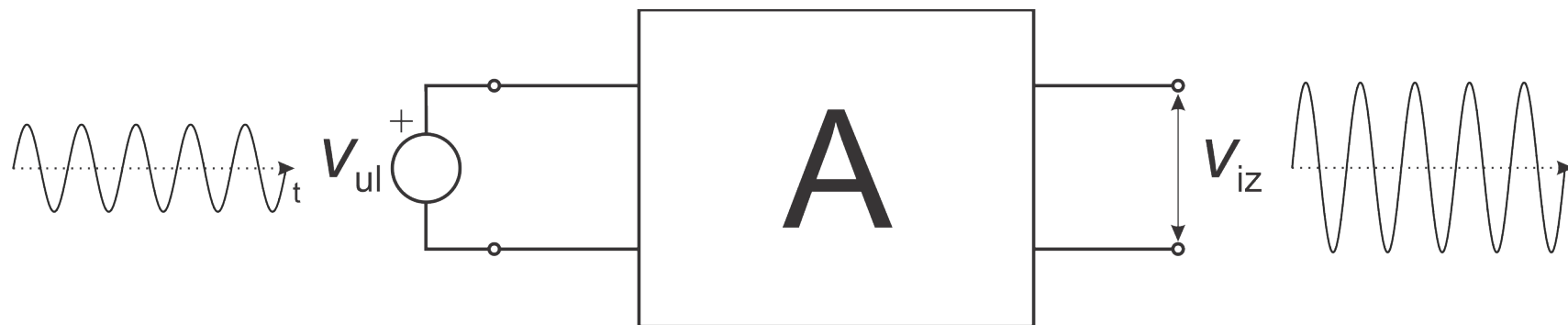
$$g_m = \frac{I_{C0}}{V_T}, \quad r_\pi = \frac{\beta \cdot V_T}{I_{C0}}, \quad r_o = \frac{V_A}{I_{C0}}$$



# Pojačavač – analiza i sinteza

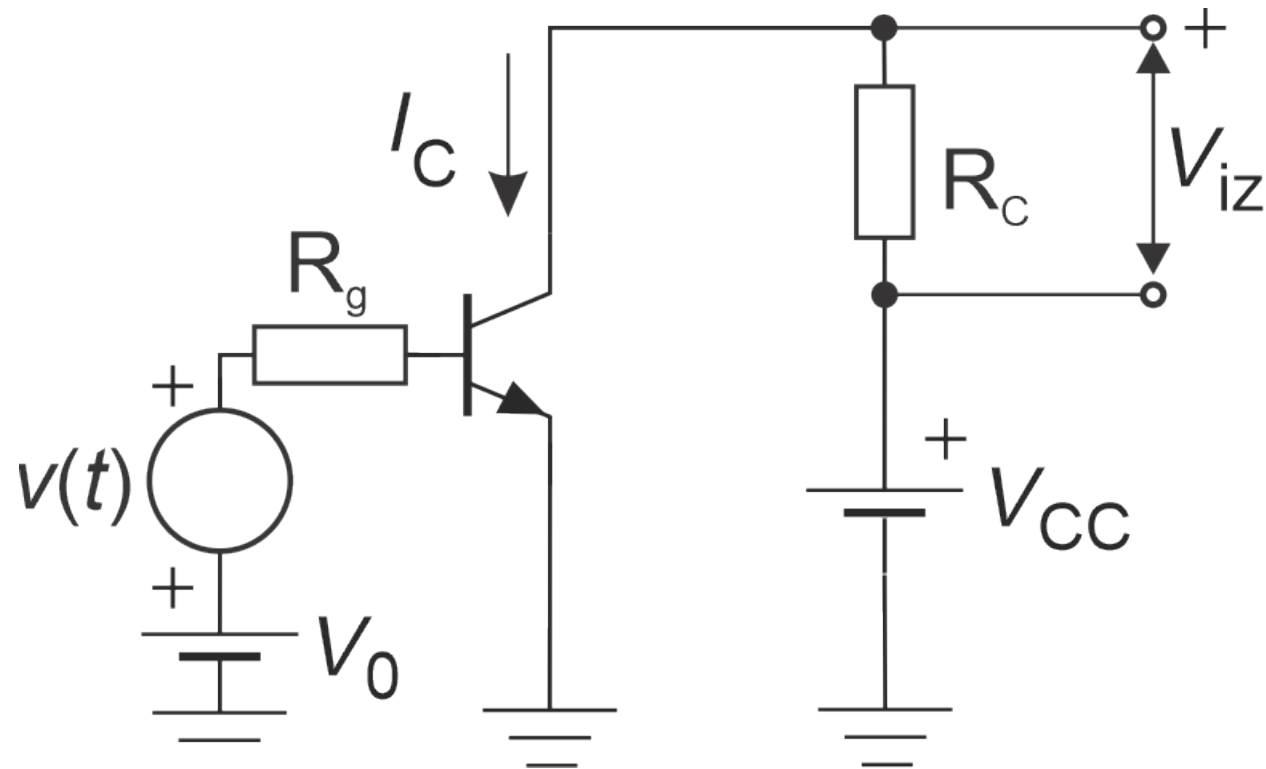
- Izbor topologije
- Obezbeđenje odgovarajuće polarizacija svih tranzistora u kolu
- Analiza ponašanja realizovanog kola za jednosmerni režim
- Analiza ponašanja realizovanog kola za male signale (pojačanje, amplitudska karakteristika, ulazna i izlazna impedansa)

# Karakteristike pojačavača

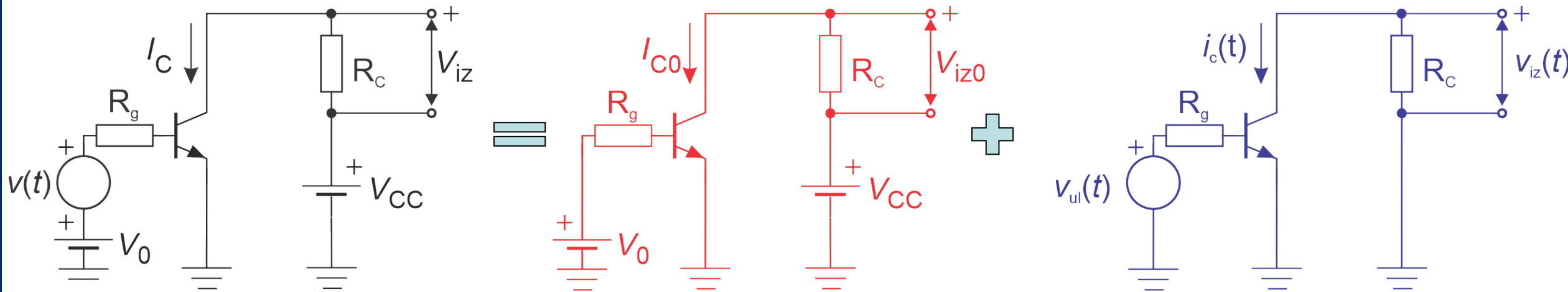


- Pojačanje  $A = v_{iz} / v_{ul}$
- Potrošnja – polarizacija tranzistora zahteva energiju
- Ulazna i izlazna impedansa
- Zavisnost od temperature
- ...

# Pojačavač sa zajedničkim emitorom



# Superpozicija – kola za velike i male signale



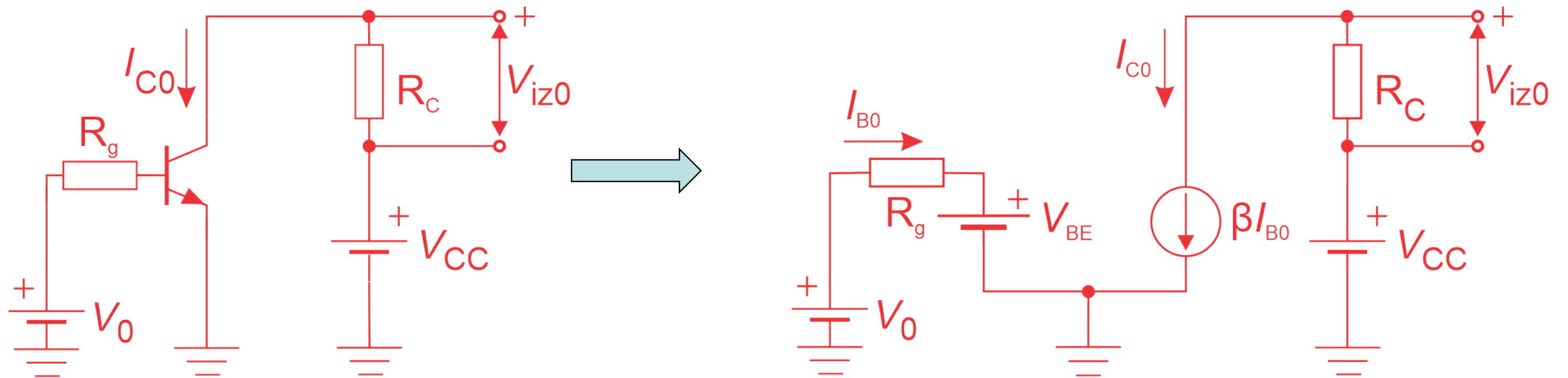
Veliki signali  
(polarizacija)

Signali malih  
amplituda



# Jednosmerni režim (veliki signali)

- Pronalazi se se  $I_{C0}$ , izračunava  $g_m$ ,  $r_{\pi}$ ,  $r_o$ .

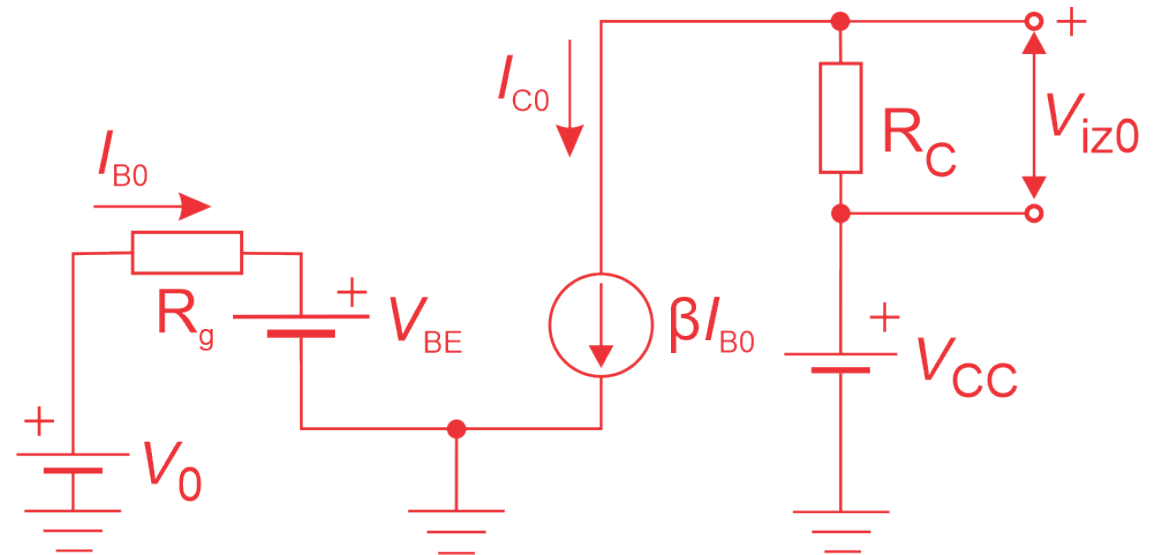


# Jednosmerni režim (veliki signali)

- $V_{BE}$ ,  $\beta$ ,  $V_A = \infty$

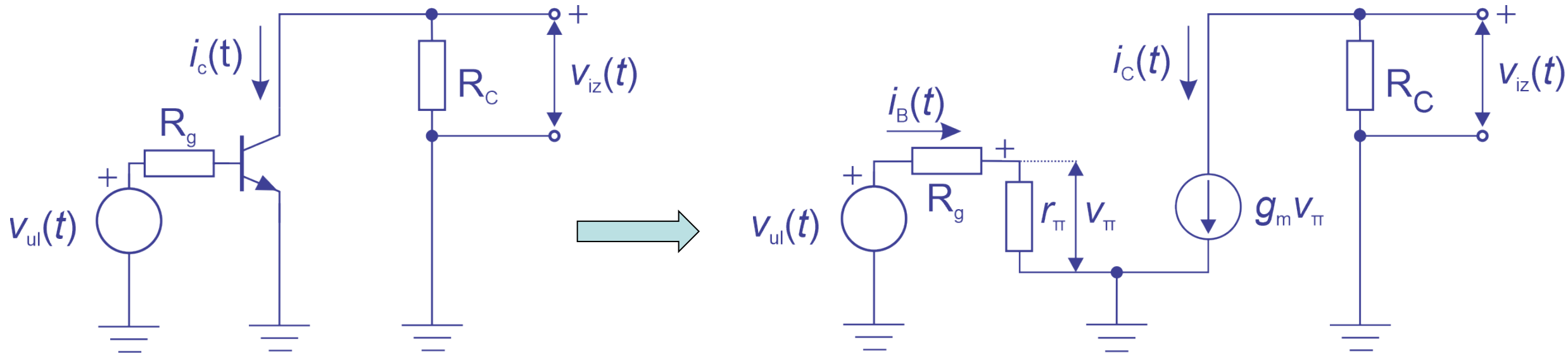
$$I_{B0} = \frac{V_0 - V_{BE}}{R_g}$$

$$I_{C0} = \beta \cdot I_{B0} = \beta \cdot \frac{V_0 - V_{BE}}{R_g}$$



# Naizmenični režim (mali signali)

- $g_m, r_{\pi}, r_o = \infty$



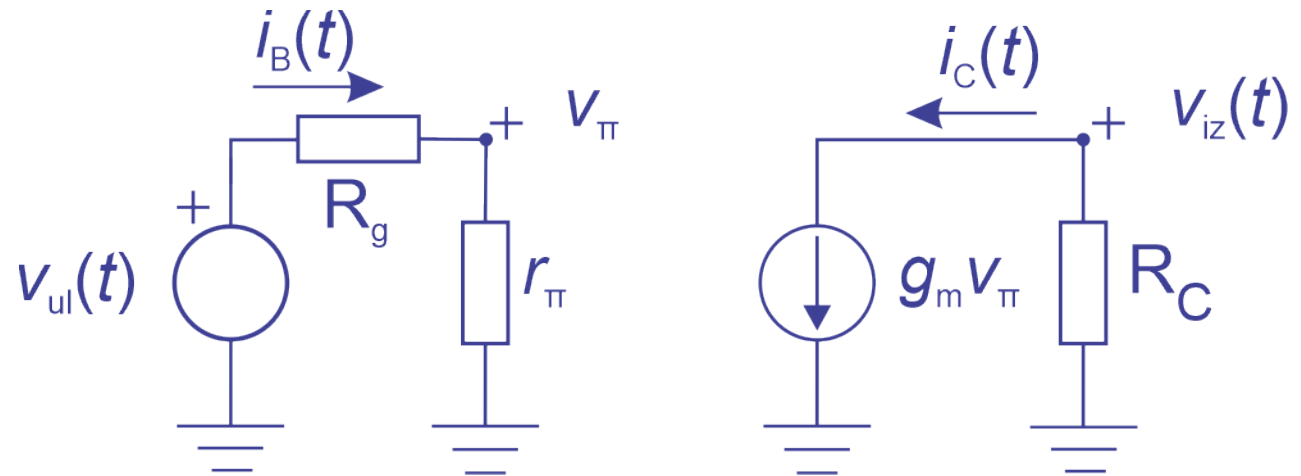
# Naizmenični režim (mali signali)

$$v_{\pi} = \frac{r_{\pi}}{r_{\pi} + R_g} \cdot v_{ul}$$

$$v_{iz} = -i_C \cdot R_C$$

$$v_{iz} = -g_m \cdot R_C \cdot v_{\pi}$$

$$v_{iz} = -g_m \cdot R_C \cdot \frac{r_{\pi}}{r_{\pi} + R_g} \cdot v_{ul}$$



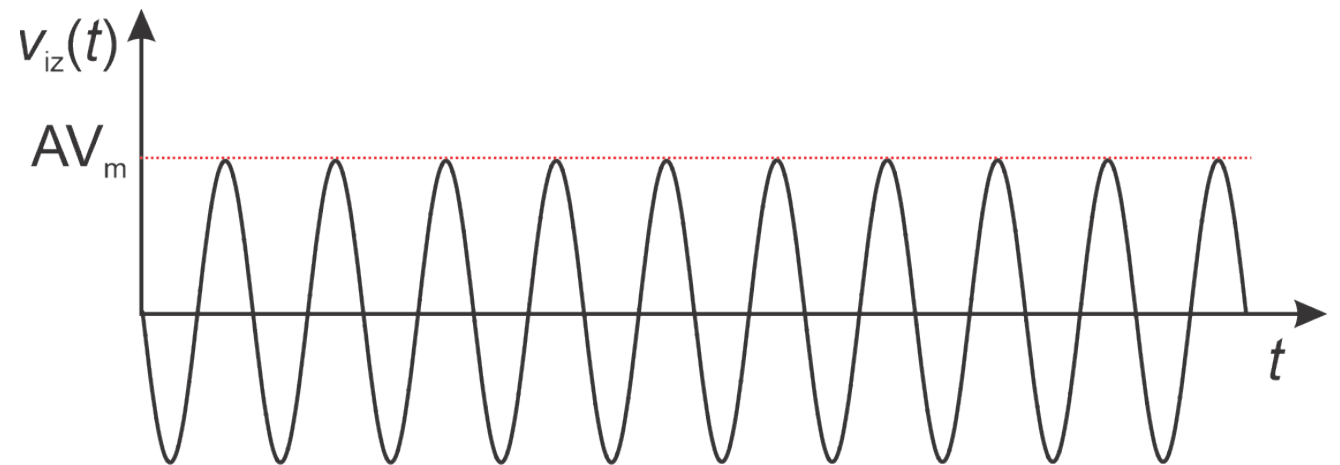
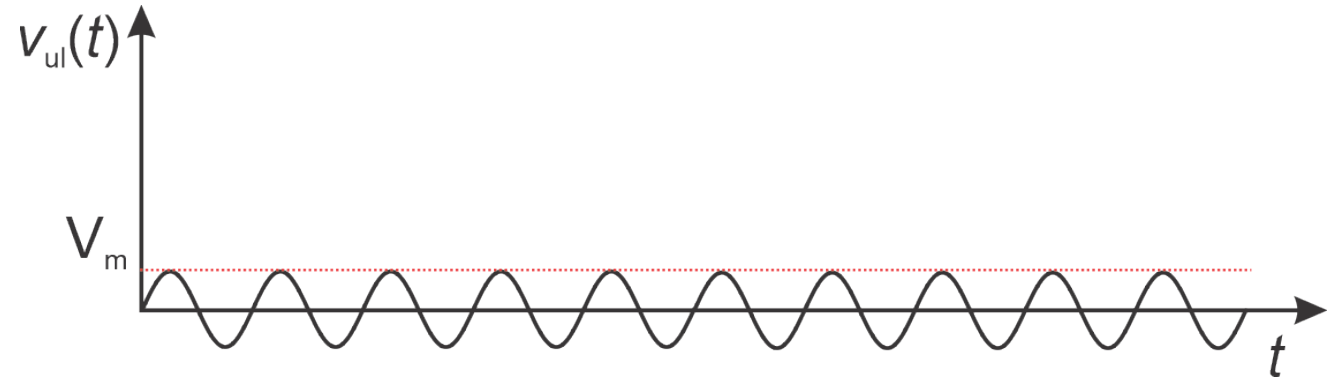
# Pojačanje pojačavača

$$A = \frac{v_{iz}}{v_{ul}}$$

$$A = -g_m \cdot R_C \cdot \frac{r_\pi}{r_\pi + R_g}$$

za  $r_\pi \gg R_g$

$$A = -g_m \cdot R_C$$

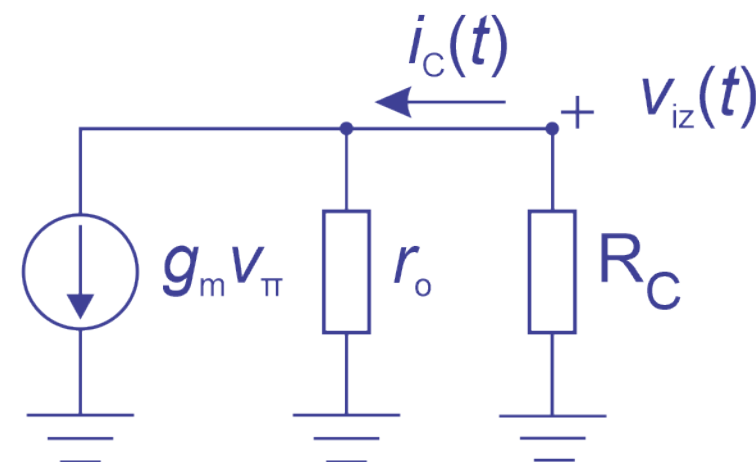
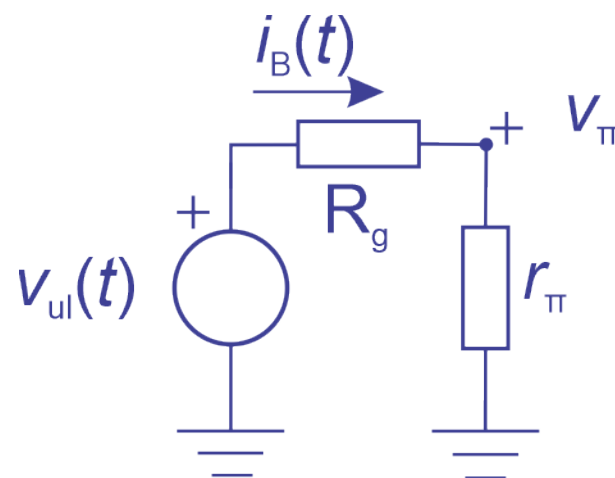


# Uticaj Erlijeovog efekta na pojačanje

$$v_{\pi} = \frac{r_{\pi}}{r_{\pi} + R_g} \cdot v_{ul}$$

$$v_{iz} = -g_m \cdot (R_C \parallel r_o) \cdot v_{\pi}$$

$$v_{iz} = -g_m \cdot (R_C \parallel r_o) \cdot \frac{r_{\pi}}{r_{\pi} + R_g} \cdot v_{ul}$$



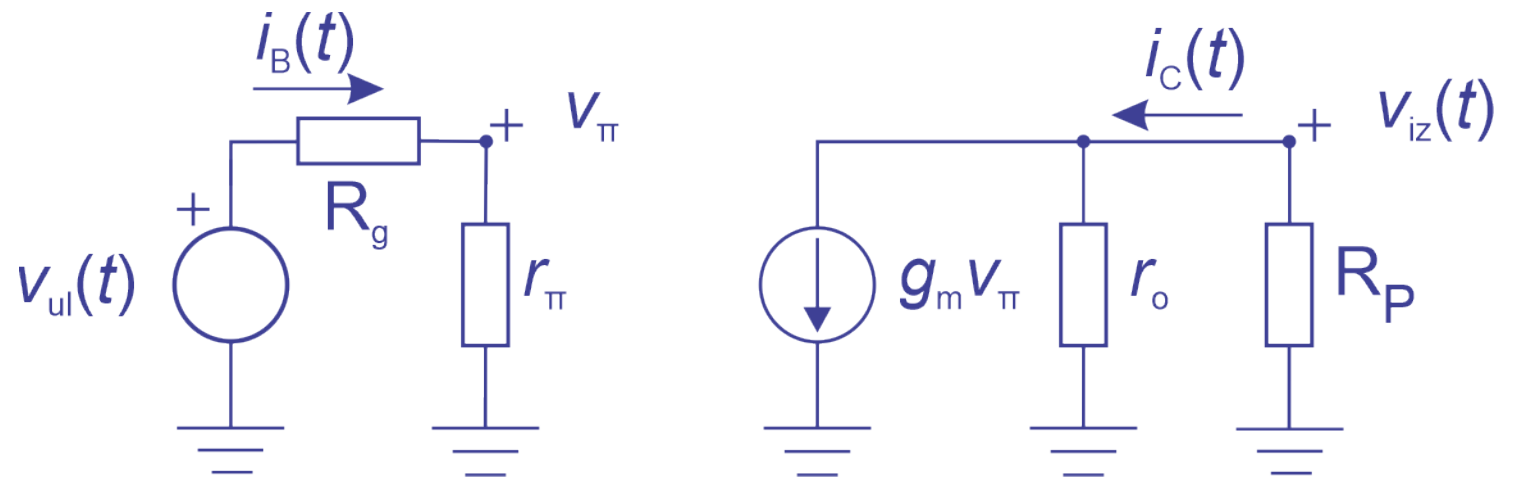
# Uticaj Erlijeovog efekta na pojačanje

$$A = \frac{v_{iz}}{v_{ul}}$$

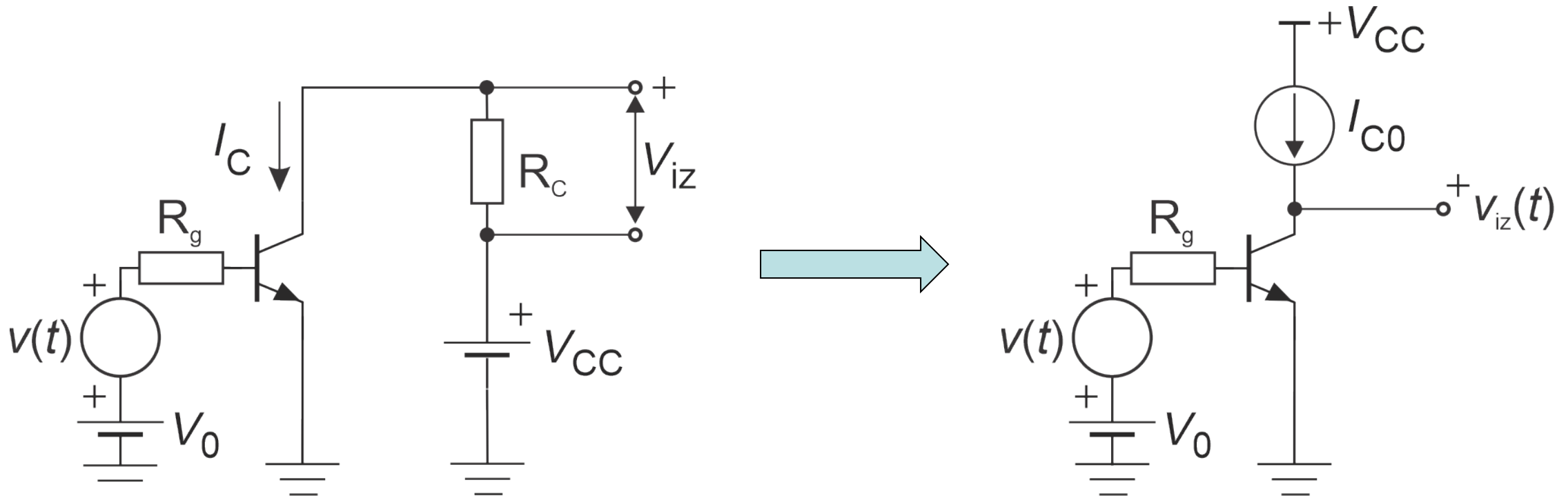
$$A = -g_m \cdot (R_C \parallel r_o) \cdot \frac{r_\pi}{r_\pi + R_g}$$

za  $r_\pi \gg R_g$

$$A = -g_m \cdot (R_C \parallel r_o)$$



# Maksimalno pojačanje pojačavača



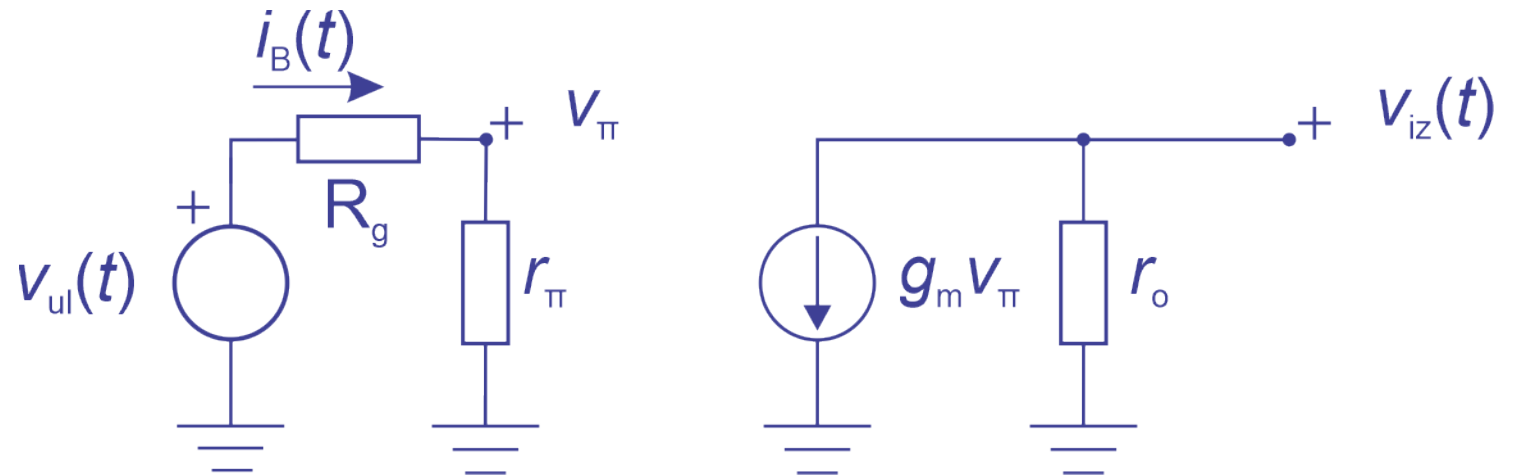


# Maksimalno pojačanje pojačavača

$$v_{\pi} = \frac{r_{\pi}}{r_{\pi} + R_g} \cdot v_{ul}$$

$$v_{iz} = -g_m \cdot r_o \cdot v_{\pi}$$

$$v_{iz} = -g_m \cdot r_o \cdot \frac{r_{\pi}}{r_{\pi} + R_g} \cdot v_{ul}$$



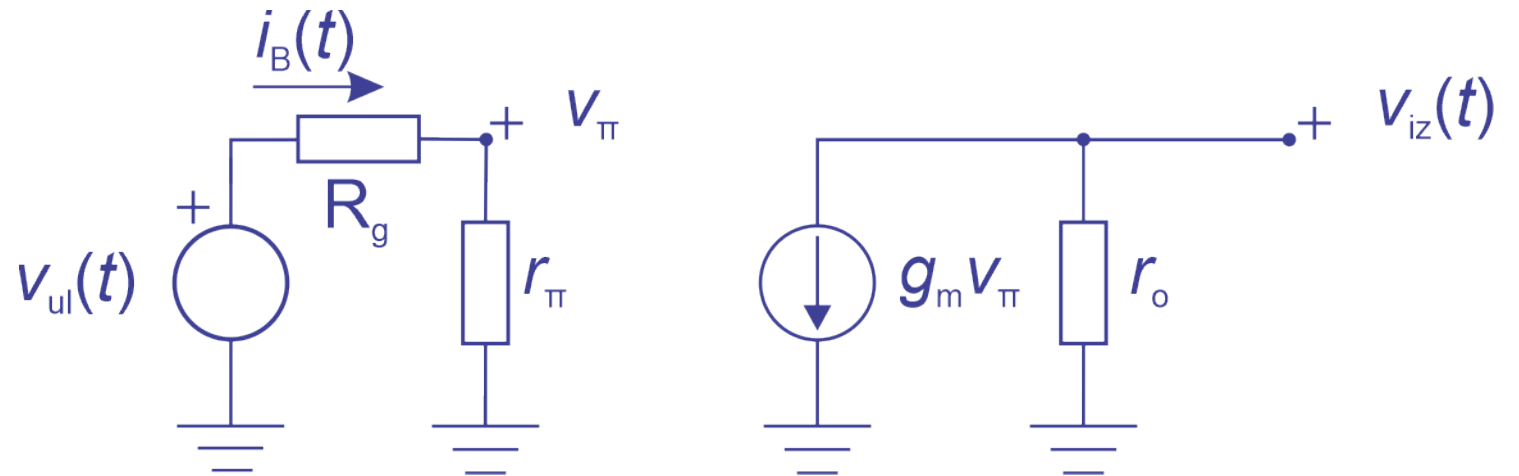
# Maksimalno pojačanje pojačavača

$$A = \frac{v_{iz}}{v_{ul}}$$

$$A = -g_m \cdot r_o \cdot \frac{r_\pi}{r_\pi + R_g}$$

za  $r_\pi \gg R_g$

$$A = -g_m \cdot r_o$$

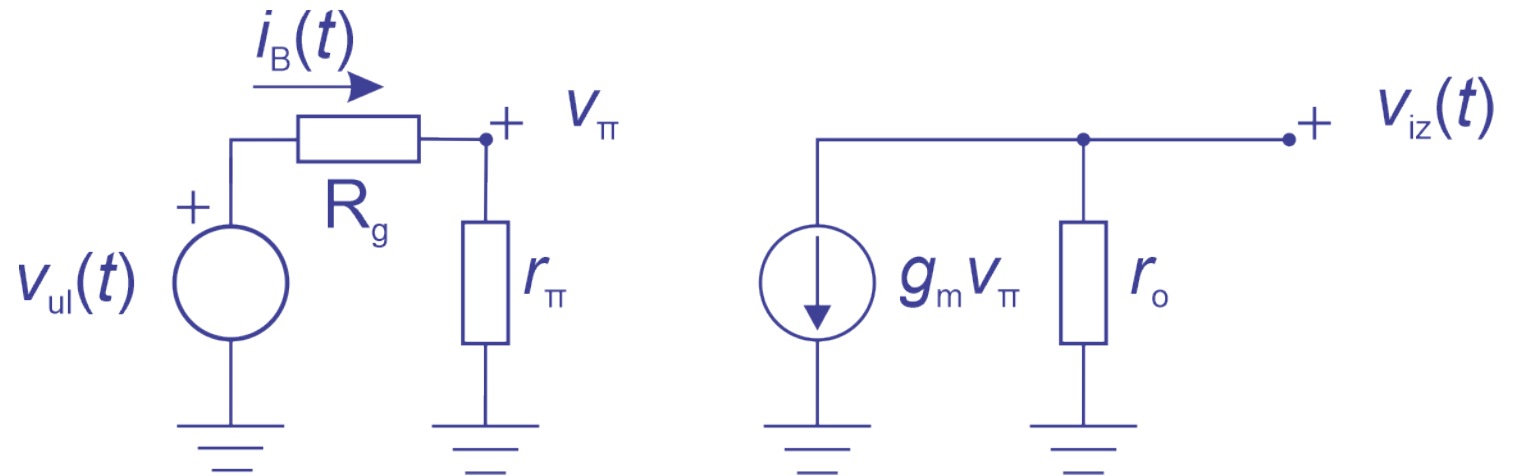


# Intrisično (maksimalno) pojačanje

$$A = -g_m \cdot r_o$$

$$A = -\frac{I_{C0}}{V_T} \cdot \frac{V_A}{I_{C0}}$$

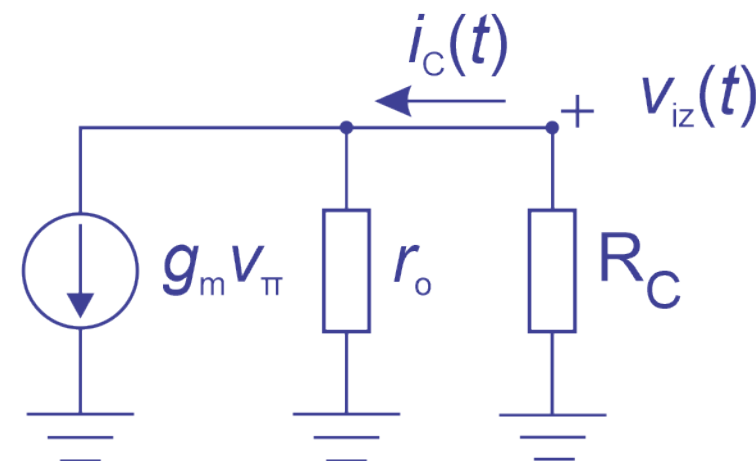
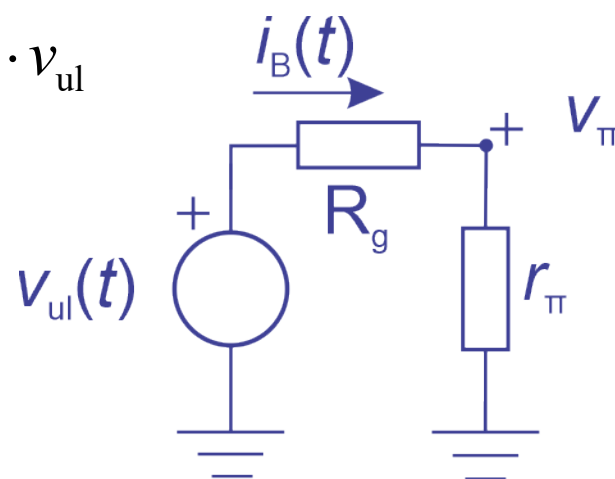
$$A = -\frac{V_A}{V_T}$$



# Ulazna impedansa

$$v_{\pi} = \frac{r_{\pi}}{r_{\pi} + R_g} \cdot v_{ul}$$

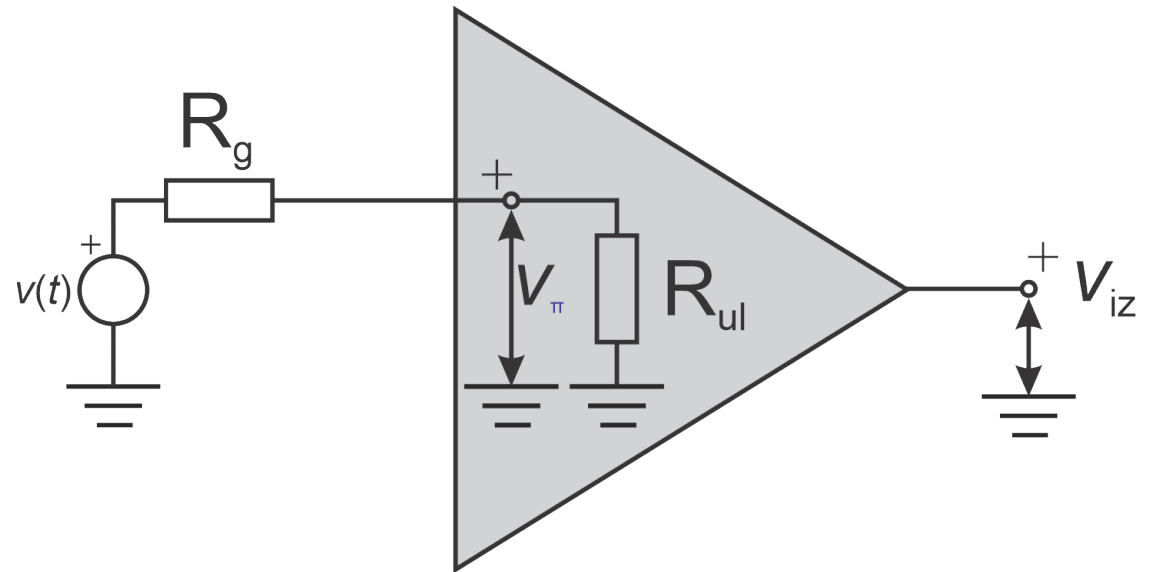
$$v_{iz} = -g_m \cdot (R_C \parallel r_o) \cdot \frac{r_{\pi}}{r_{\pi} + R_g} \cdot v_{ul}$$



# Ulazna impedansa

$$v_{\pi} = \frac{r_{\pi}}{r_{\pi} + R_g} \cdot v_{ul}$$

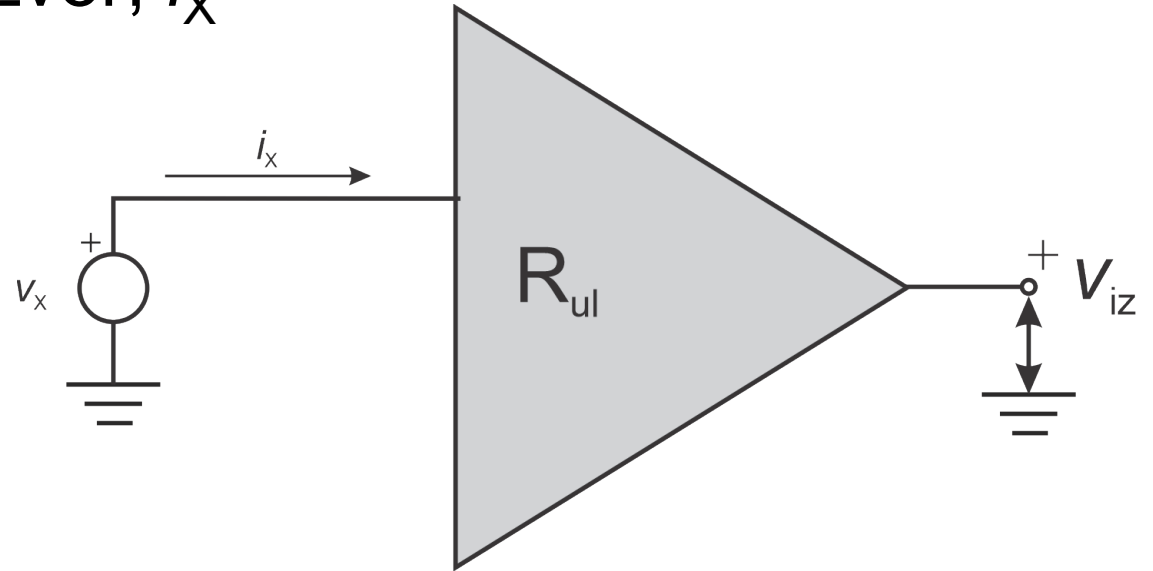
$$v_{iz} = -g_m \cdot (R_C \parallel r_o) \cdot \frac{r_{\pi}}{r_{\pi} + R_g} \cdot v_{ul}$$



# Ulazna impedansa

- Kratkospojiti sve nezavisne naponske generatore
- Odvezati sve nezavisne strujne generatore
- Postaviti izvor malog signala na ulaz kola  $v_x$
- Izračunati struju koju proizvodi izvor,  $i_x$

$$R_{ul} = \frac{v_x}{i_x}$$

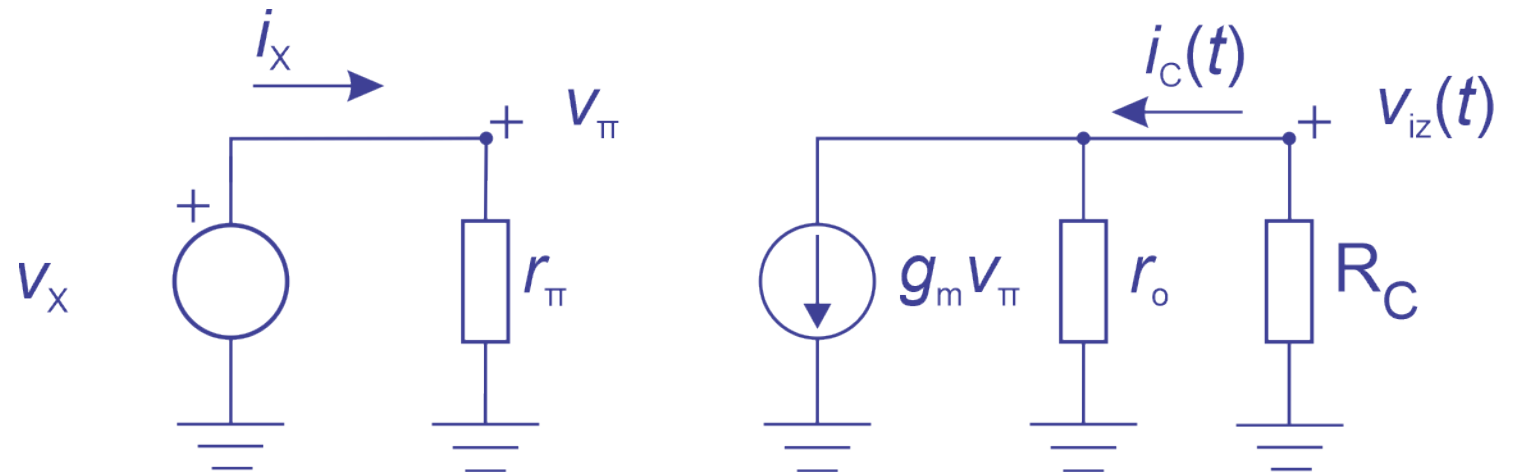


# Ulazna impedansa

$$i_X = \frac{v_X}{r_\pi}$$

$$R_{ul} = \frac{v_X}{i_X}$$

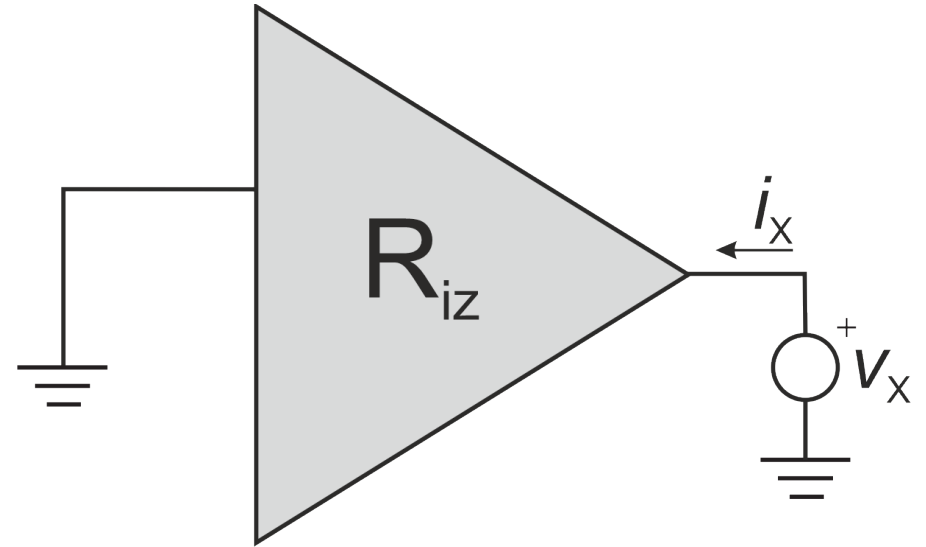
$$R_{ul} = r_\pi$$



# Izlazna impedansa

- Kratkospojiti sve nezavisne naponske generatore
- Odvezati sve nezavisne strujne generatore
- Odrediti ekvivalentnu Thevenenovu otpornost kola

$$R_{iz} = \frac{v_X}{i_X}$$



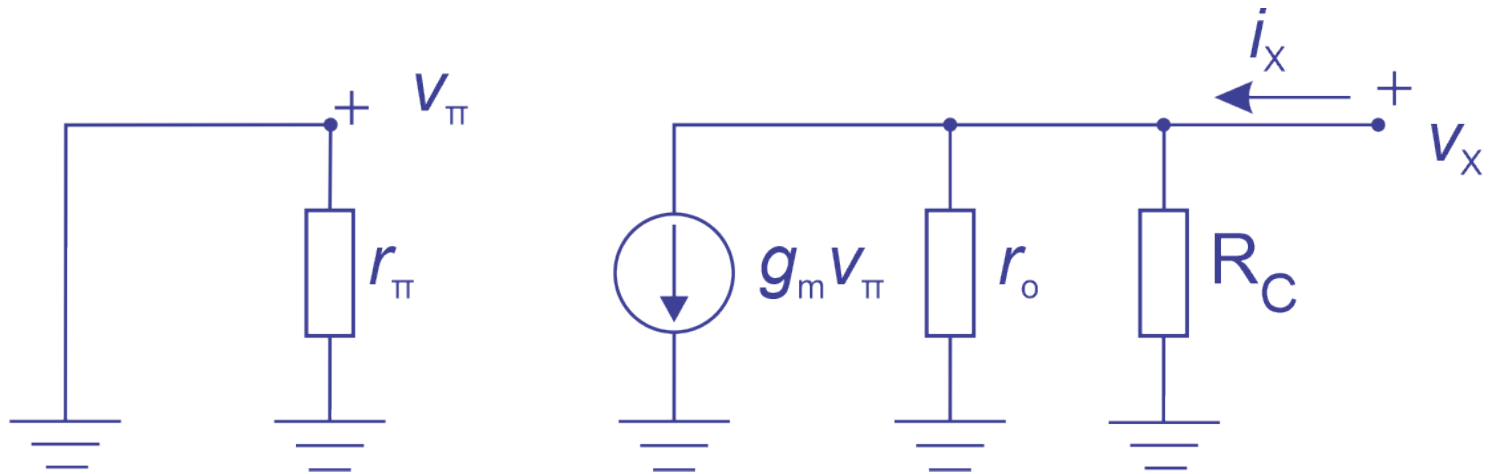


# Izlazna impedansa

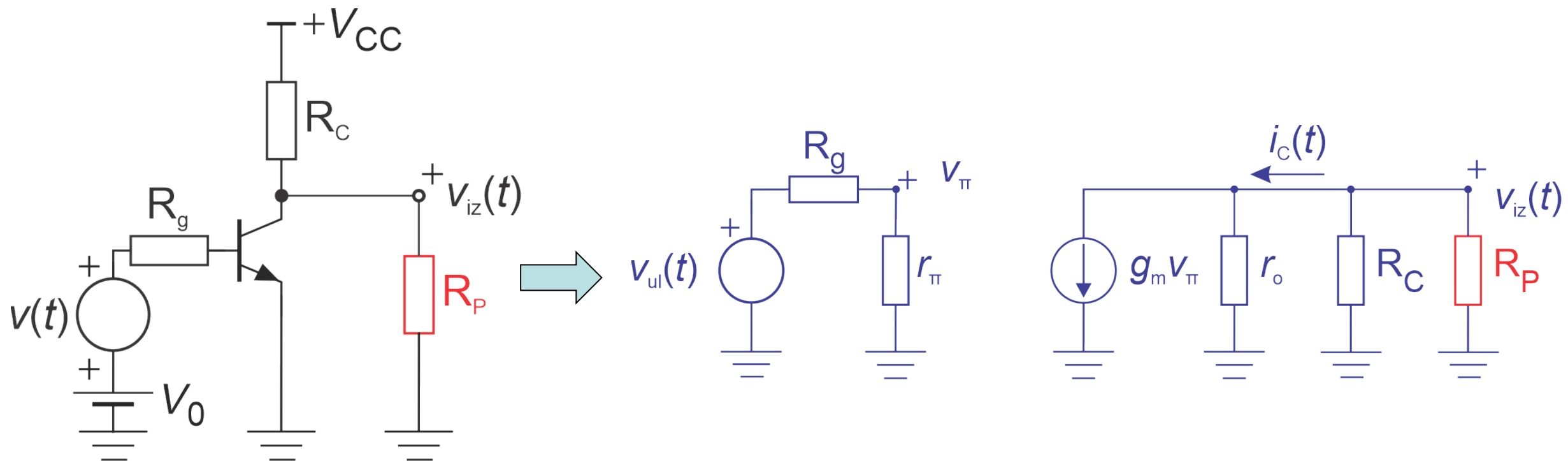
$$v_{\pi} = 0$$

$$v_X = i_X \cdot r_o \parallel R_C$$

$$R_{iz} = r_o \parallel R_C$$



# Uticaj otpornosti potrošača



# Uticaj otpornosti potrošača

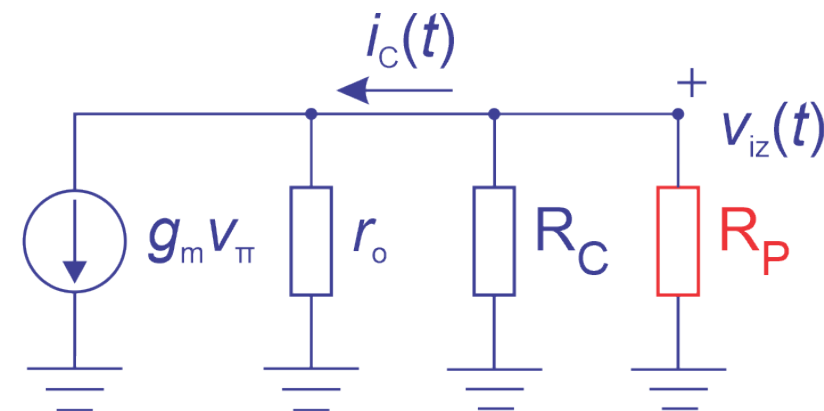
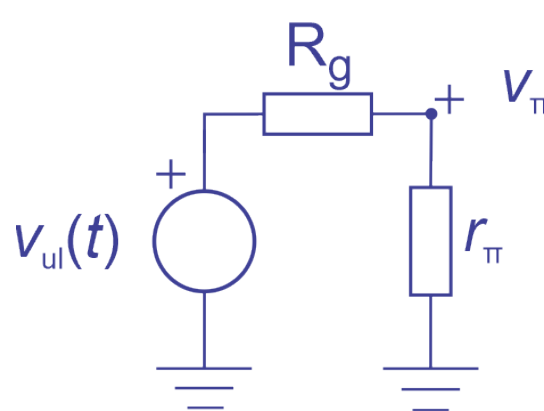
$$v_{\pi} = \frac{r_{\pi}}{r_{\pi} + R_g} \cdot v_{ul}$$

$$v_{iz} = -g_m \cdot (R_C \parallel r_o \parallel R_P) \cdot \frac{r_{\pi}}{r_{\pi} + R_g} \cdot v_{ul}$$

$$A = -g_m \cdot (R_C \parallel r_o \parallel R_P) \cdot \frac{r_{\pi}}{r_{pi} + R_g}$$

za  $r_{\pi} \gg R_g$

$$A = -g_m \cdot (R_C \parallel r_o \parallel R_P)$$



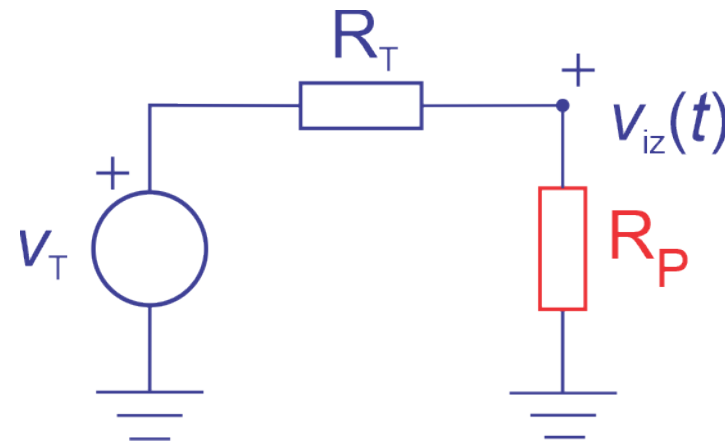
# Uticaj otpornosti potrošača

$$v_T = -g_m \cdot v_\pi \cdot (R_C \parallel r_o) \quad R_T = R_C \parallel r_o$$

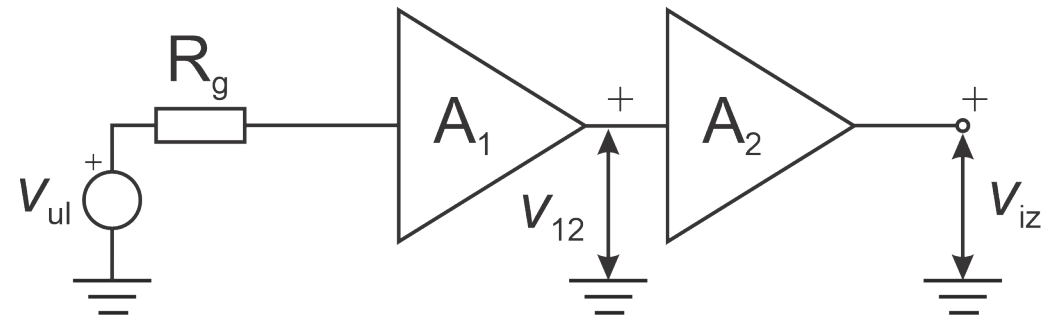
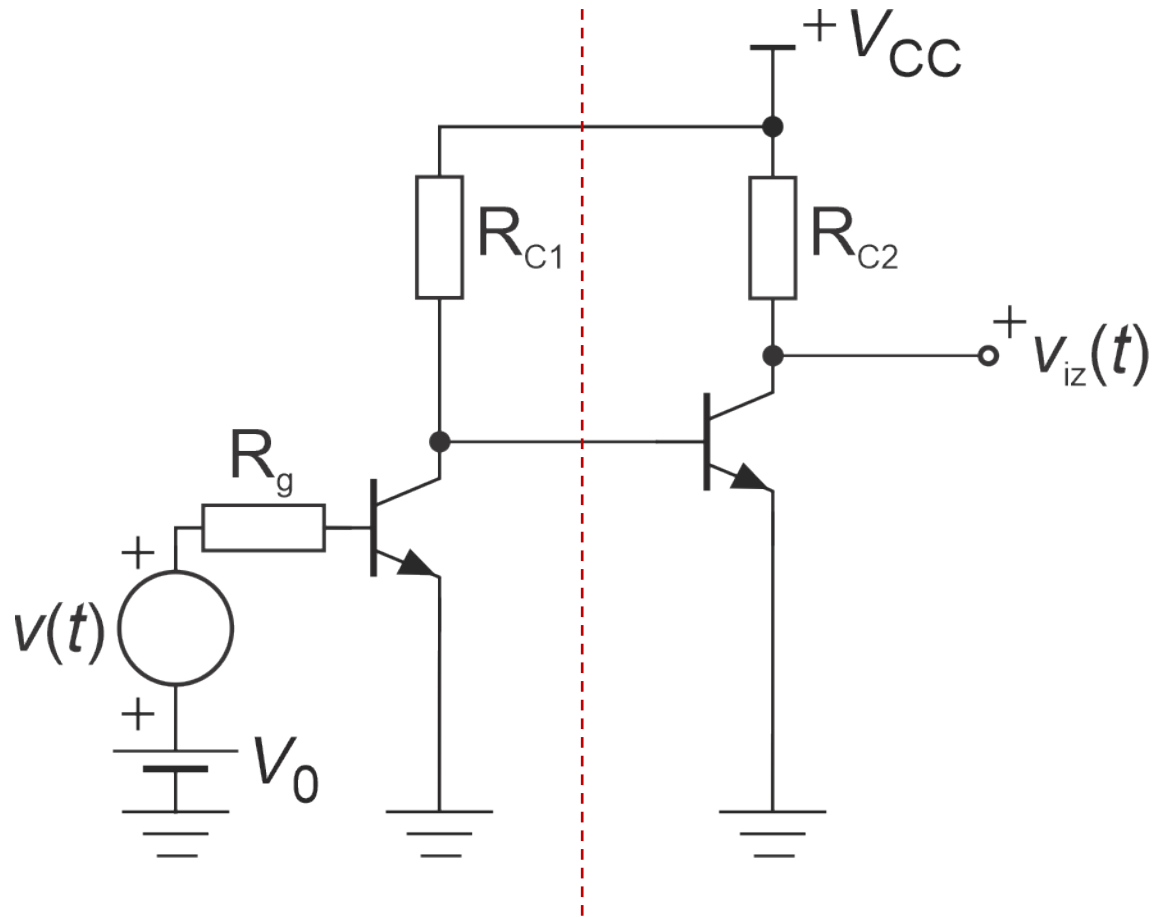
$$v_{iz} = \frac{R_P}{R_T + R_P} \cdot v_T$$

$$v_{iz} = -g_m \cdot v_\pi \cdot \frac{R_P R_C r_o}{R_C r_o + R_C R_P + r_o R_P}$$

$$v_{iz} = -g_m \cdot (R_C \parallel r_o \parallel R_P) \cdot \frac{r_\pi}{r_\pi + R_g} \cdot v_{ul}$$

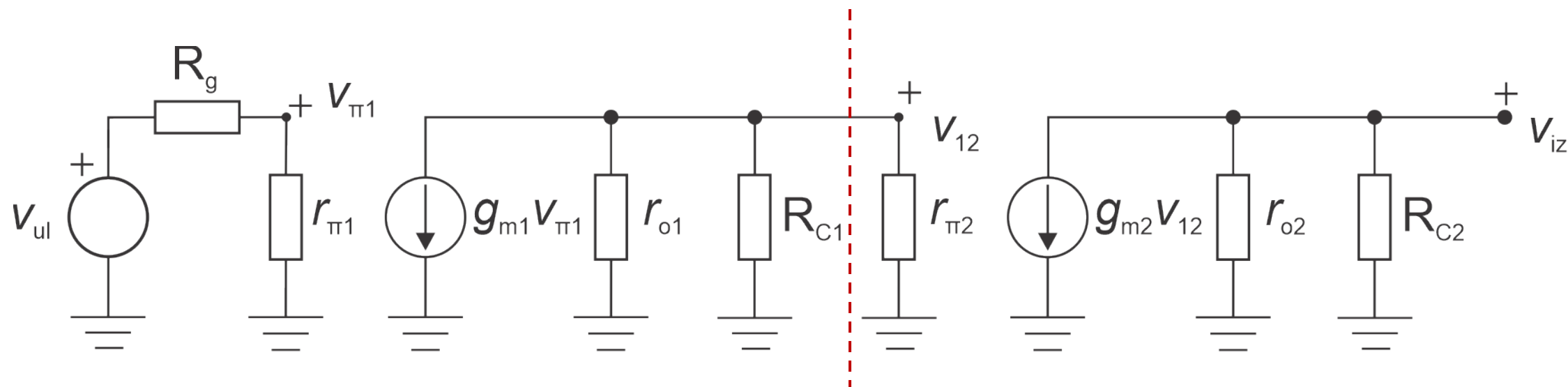


# Kaskadna veza pojačavača



$$A = A_1 A_2?$$

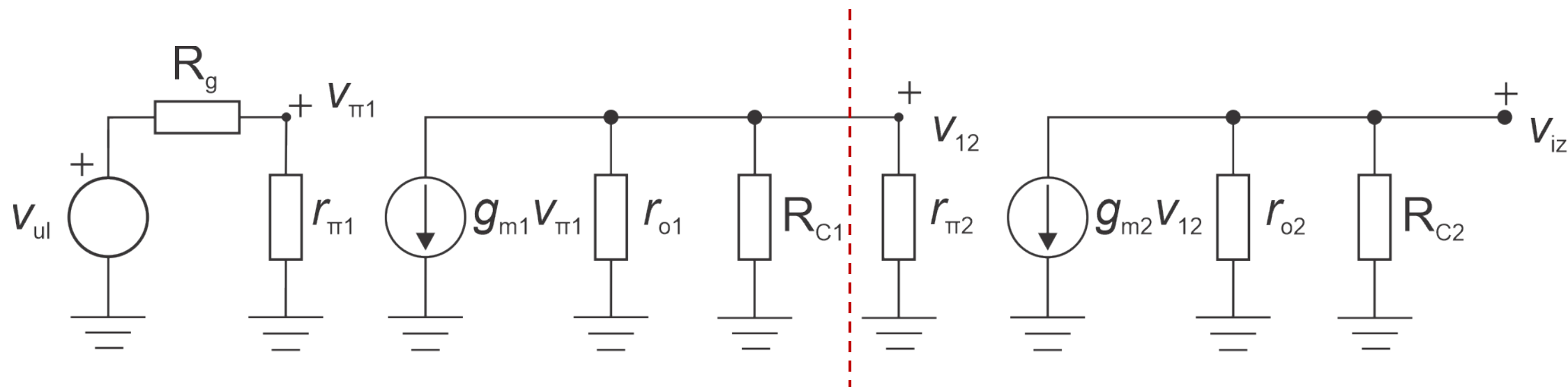
# Kaskadna veza pojačavača



$$v_{12} = -g_{m1} \cdot (r_{o1} \parallel R_{C1} \parallel r_{\pi 2}) \cdot \frac{r_{\pi}}{r_{\pi} + R_g} \cdot v_{ul}$$

$$v_{iz} = -g_{m2} \cdot (r_{o2} \parallel R_{C2}) \cdot v_{12}$$

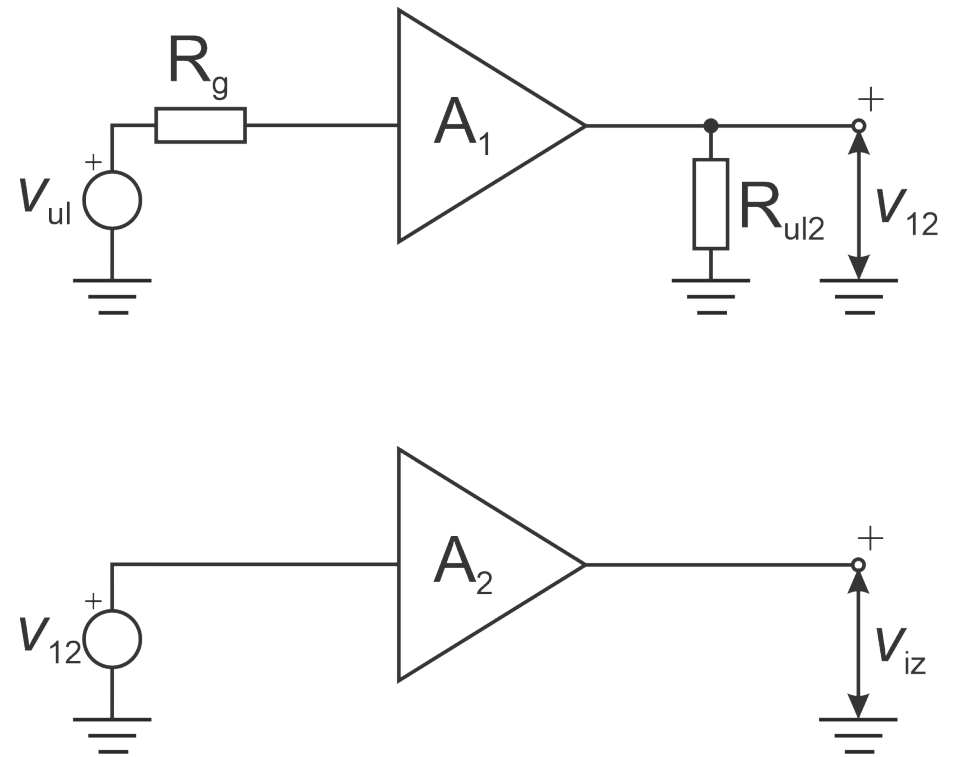
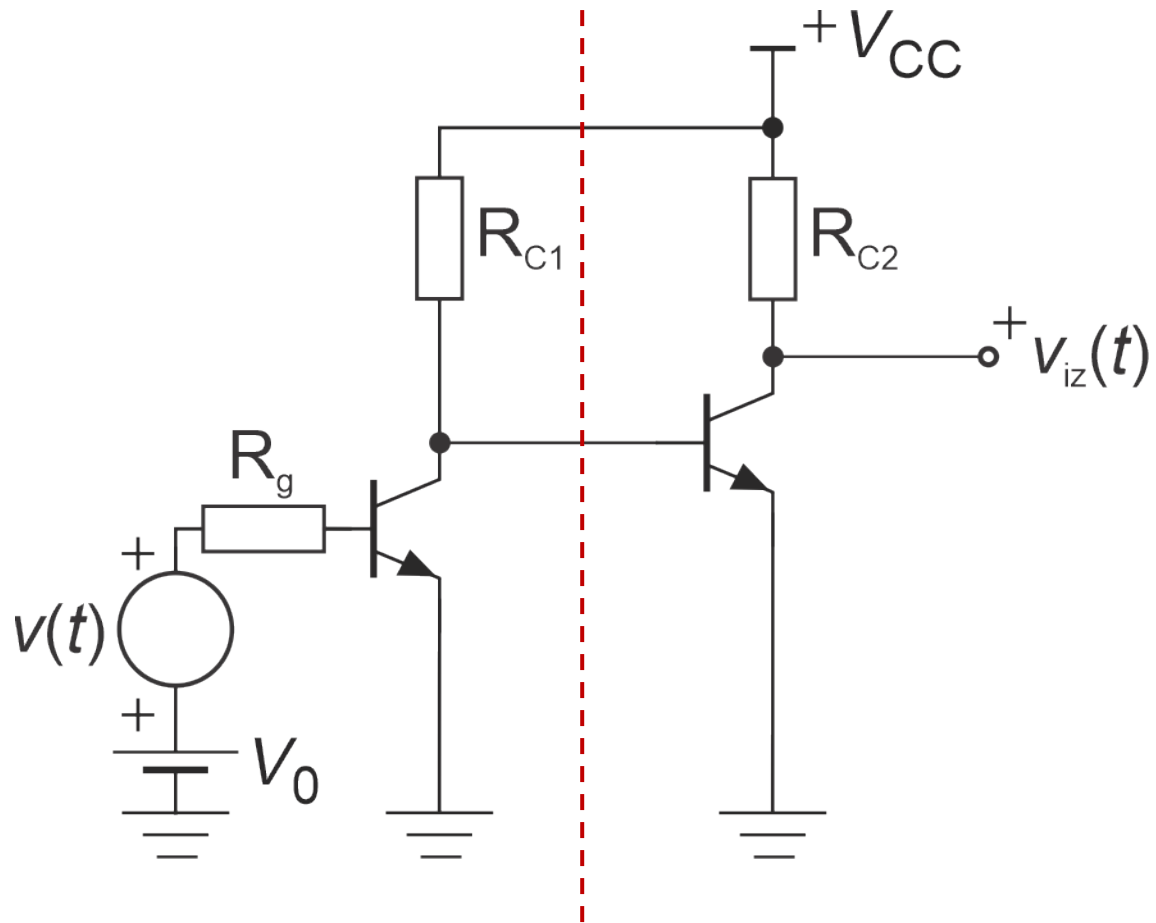
# Kaskadna veza pojačavača



$$A_1 = -g_{m1} \cdot (r_{o1} \parallel R_{C1} \parallel r_{\pi2}) \cdot \frac{r_{\pi}}{r_{\pi} + R_g}$$

$$A_2 = -g_{m2} \cdot (r_{o2} \parallel R_{C2})$$

# Kaskadna veza pojačavača





# Temperaturna zavisnost pojačavača

- Varijacija pojačanja usled promene temperature:

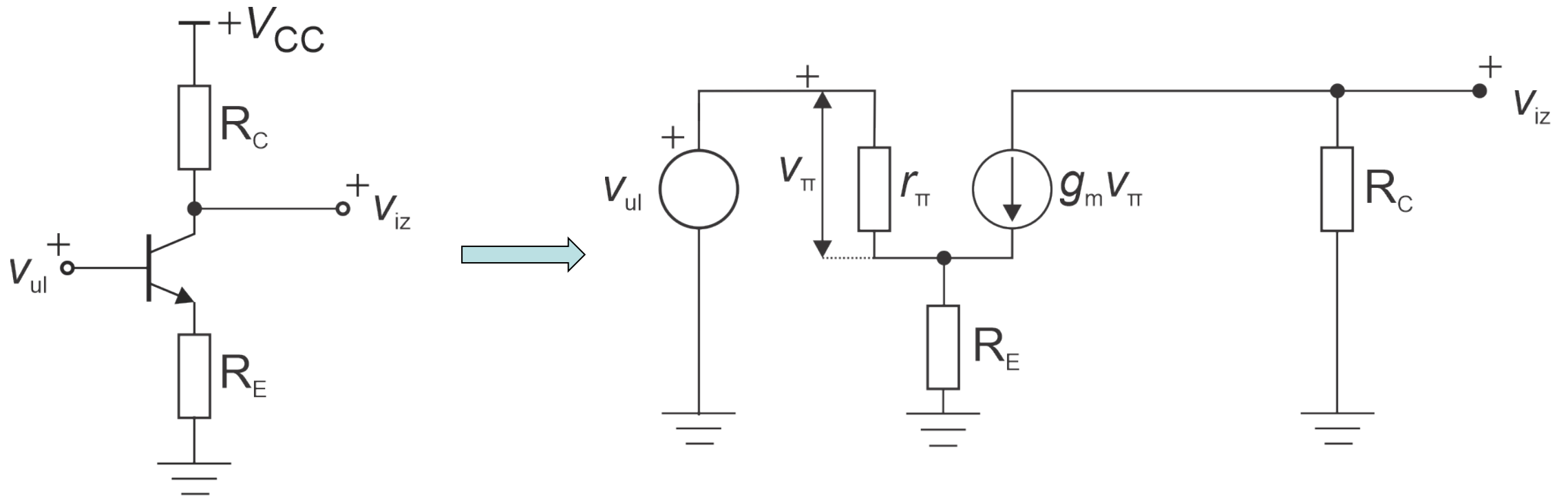
$$A = -g_m \cdot (r_o \parallel R_C)$$

$$g_m = \frac{I_{C0}}{V_T}, \quad I_{C0} = I_S \exp\left(\frac{V_{BE}}{V_T}\right), \quad V_T = \frac{kT}{q_e}$$

$$I_S \sim n_i^2 \sim T^3 \exp\left(-\frac{\epsilon_g}{kT}\right) \quad g_m \sim T^2 \exp\left(\frac{q_e V_{BE} - \epsilon_g}{kT}\right)$$

# Degenerisani emitor

- Otpornik u grani emitora ( $r_o = \infty$ )

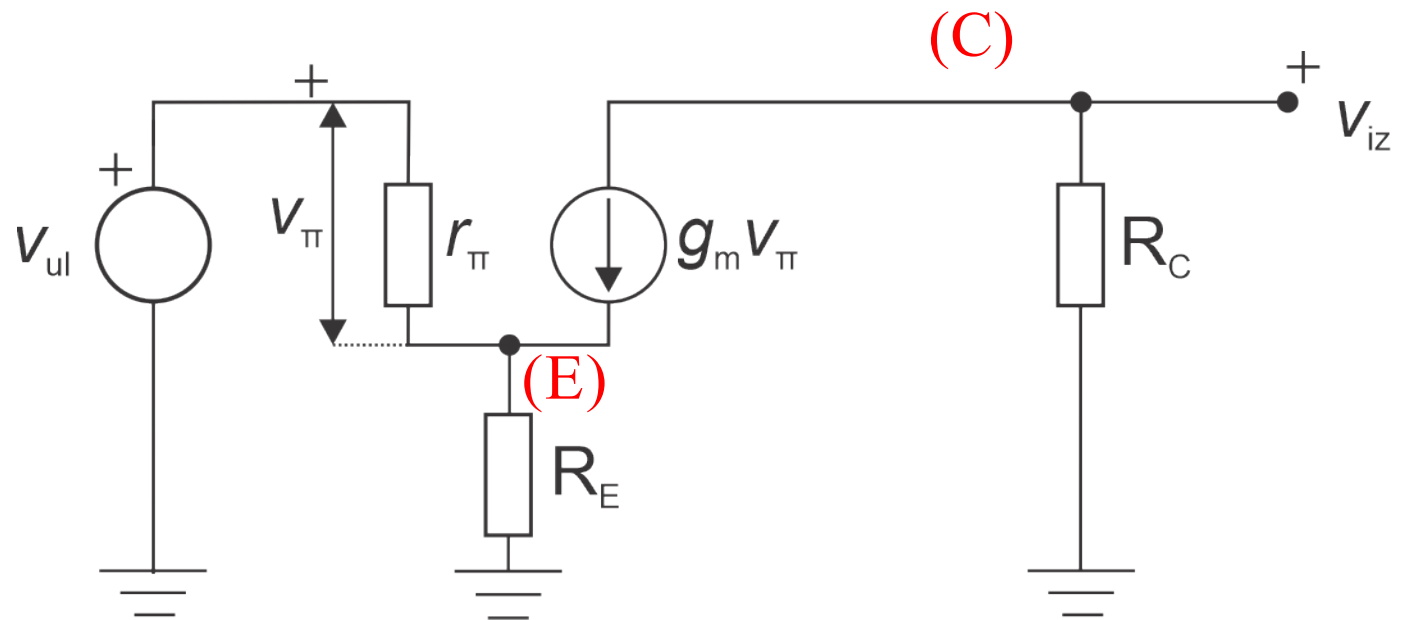


# Degenerisani emitor – pojačanje

$$\frac{v_{iz}}{R_C} + g_m \cdot v_\pi = 0 \quad (C)$$

$$v_\pi = -\frac{v_{iz}}{g_m \cdot R_C}$$

$$\frac{v_{ul} - v_\pi}{R_E} = g_m \cdot v_\pi + \frac{v_\pi}{r_\pi} \quad (E)$$

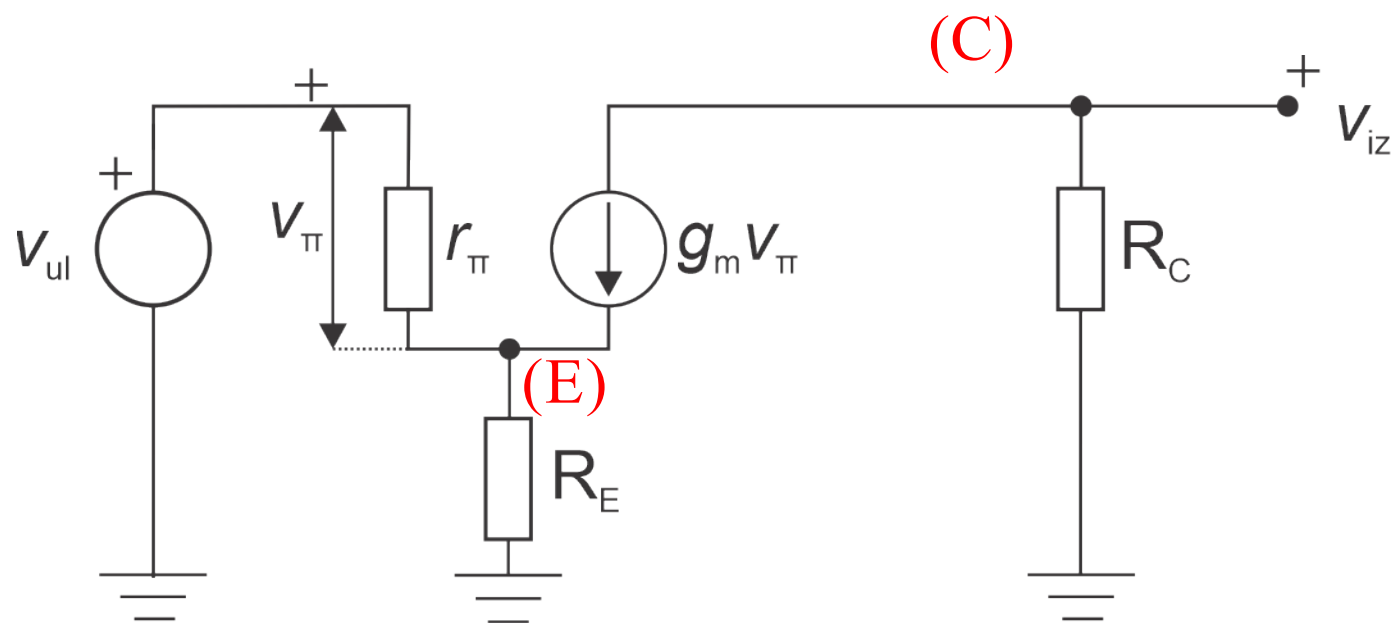


# Degenerisani emitor – pojačanje

$$v_{ul} = \left( g_m R_E + \frac{R_E}{r_\pi} + 1 \right) v_\pi$$

$$v_{ul} = - \frac{g_m R_E + \frac{R_E}{r_\pi} + 1}{g_m \cdot R_C} v_{iz}$$

$$v_{iz} = - \frac{g_m R_C r_\pi}{g_m R_E r_\pi + R_E + r_\pi} v_{ul}$$



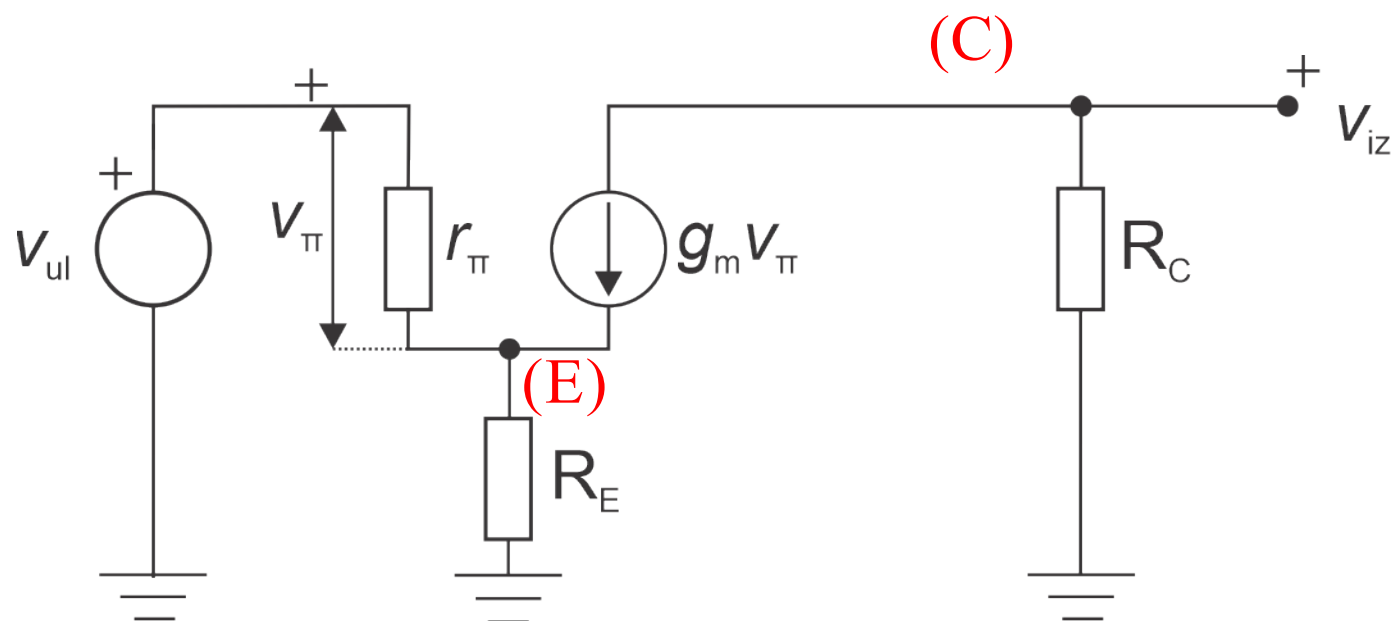
# Degenerisani emitor – pojačanje

$$v_{iz} = -\frac{\beta R_C}{R_E (1 + \beta) + r_\pi} v_{ul} \quad (\cdot g_m)$$

$$v_{iz} = -\frac{\beta g_m R_C}{R_E g_m (1 + \beta) + \beta} v_{ul}$$

$$A = -\frac{\beta g_m R_C}{R_E g_m (1 + \beta) + \beta}$$

$$A \approx -\frac{g_m R_C}{1 + g_m R_E}$$

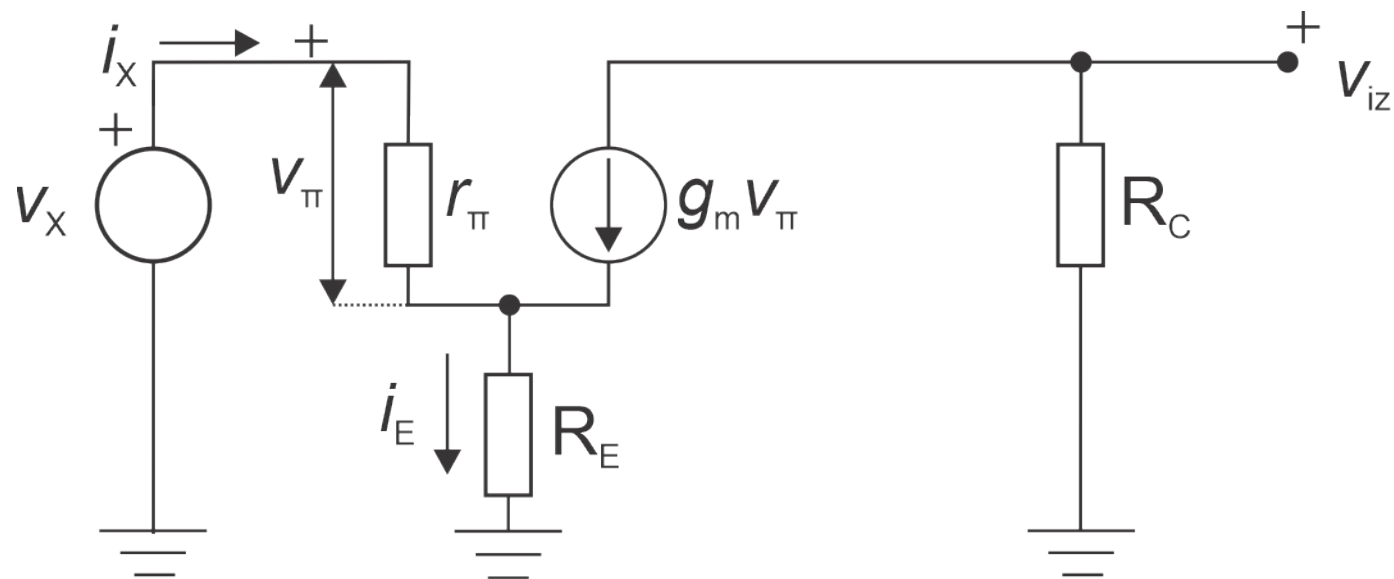


# Degenerisani emitor – ulazna impedansa

$$i_E = (\beta + 1)i_X$$

$$v_X = R_E \cdot (\beta + 1)i_X + r_\pi i_X$$

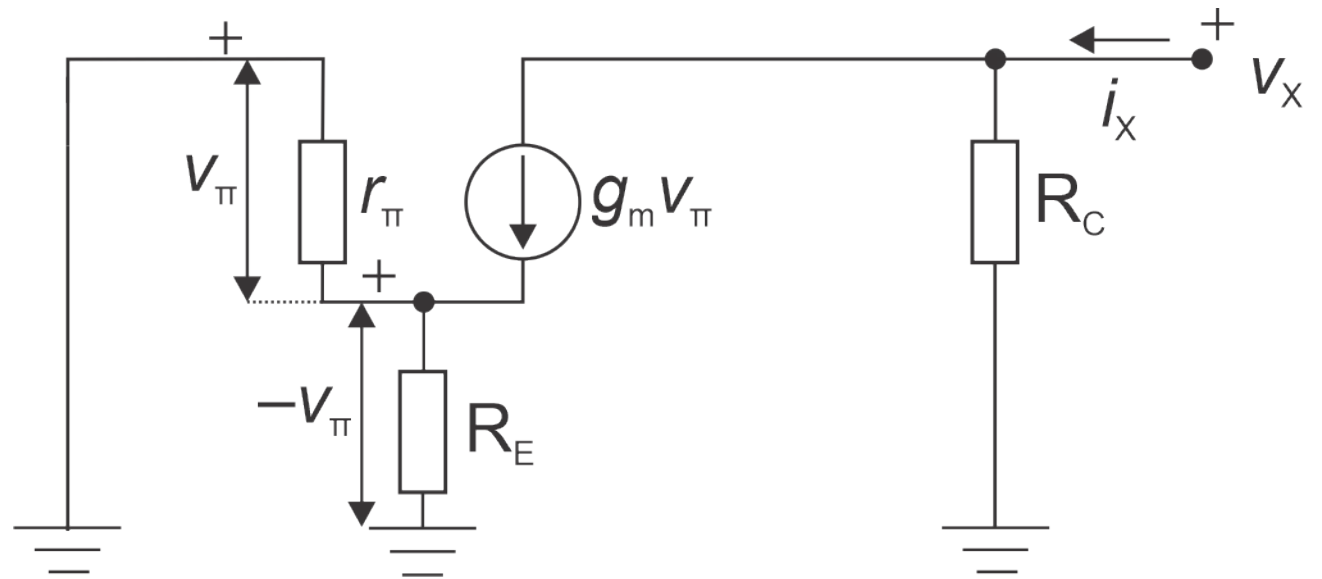
$$R_{ul} = \frac{v_X}{i_X} = (\beta + 1)R_E + r_\pi$$



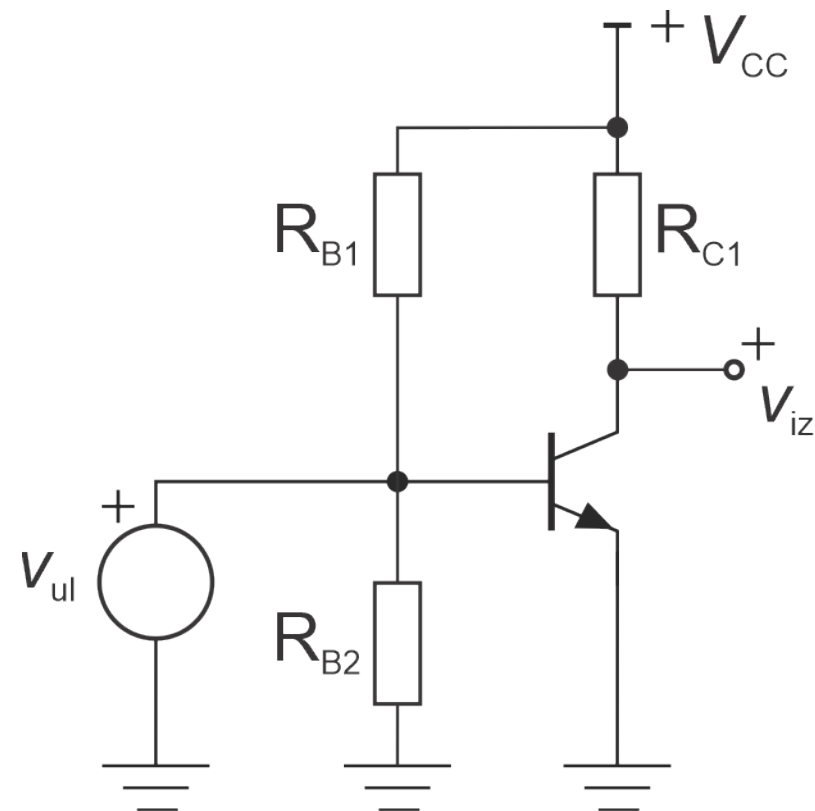
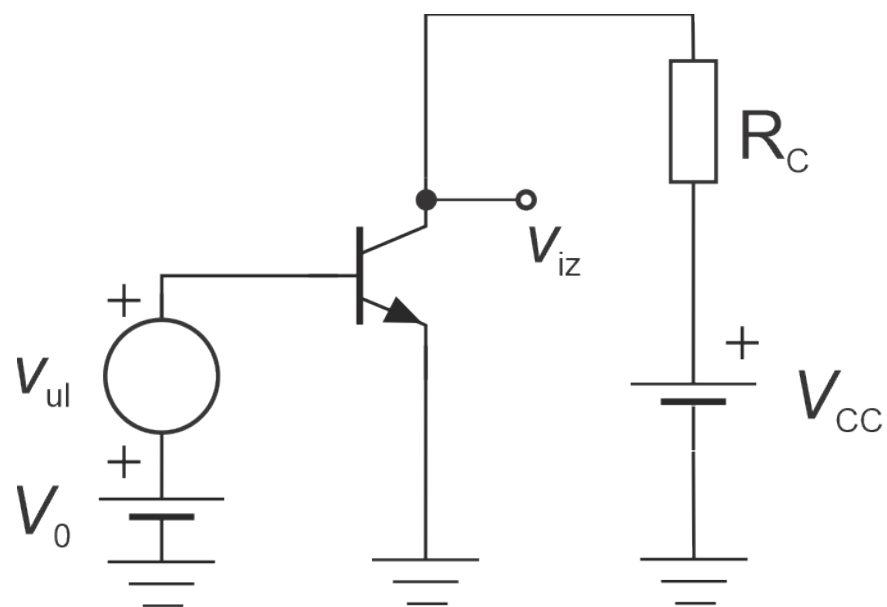
# Degenerisani emitor – izlazna impedansa

$$\frac{v_{\pi}}{r_{\pi}} + g_m v_{\pi} = -R_E v_{\pi} \Rightarrow v_{\pi} = 0$$

$$R_{iz} = \frac{v_X}{i_X} = R_C$$



# Kola za polarizaciju



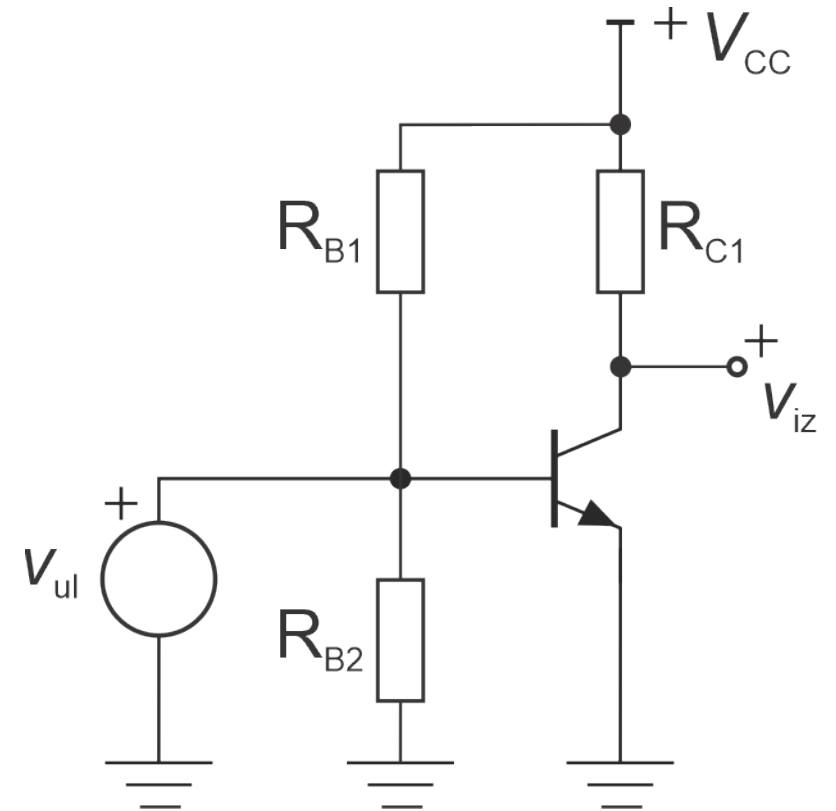


# Kola za polarizaciju

$$I_{B1} = \frac{V_{CC} - V_{BE}}{R_{B1}}$$

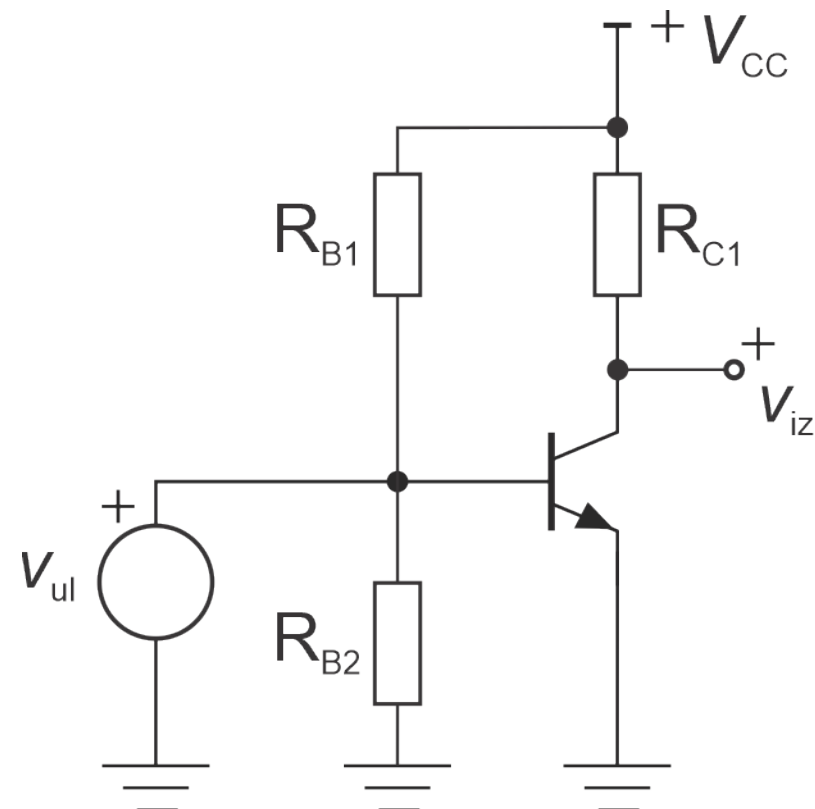
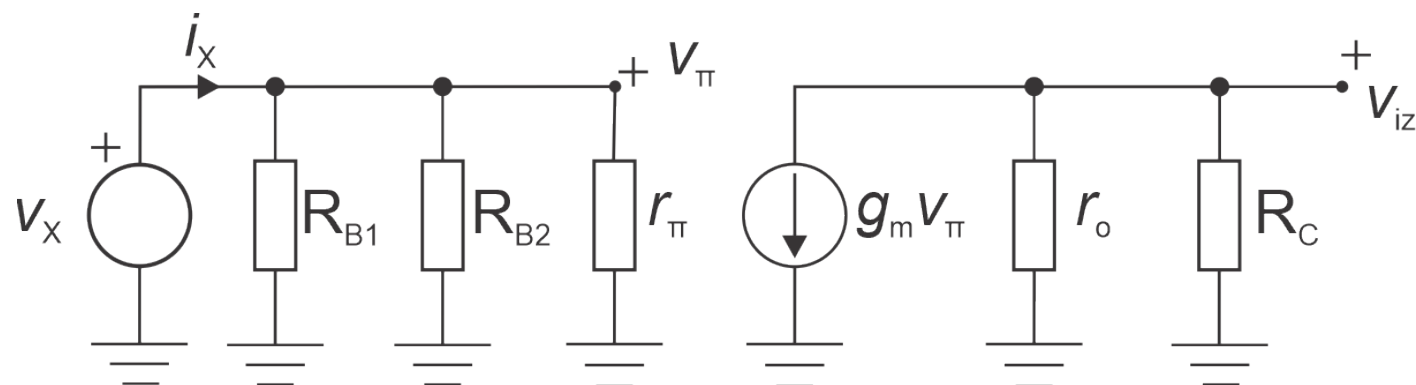
$$I_{B2} = \frac{V_{BE}}{R_{B2}}$$

$$I_B = I_{B1} - I_{B2}$$



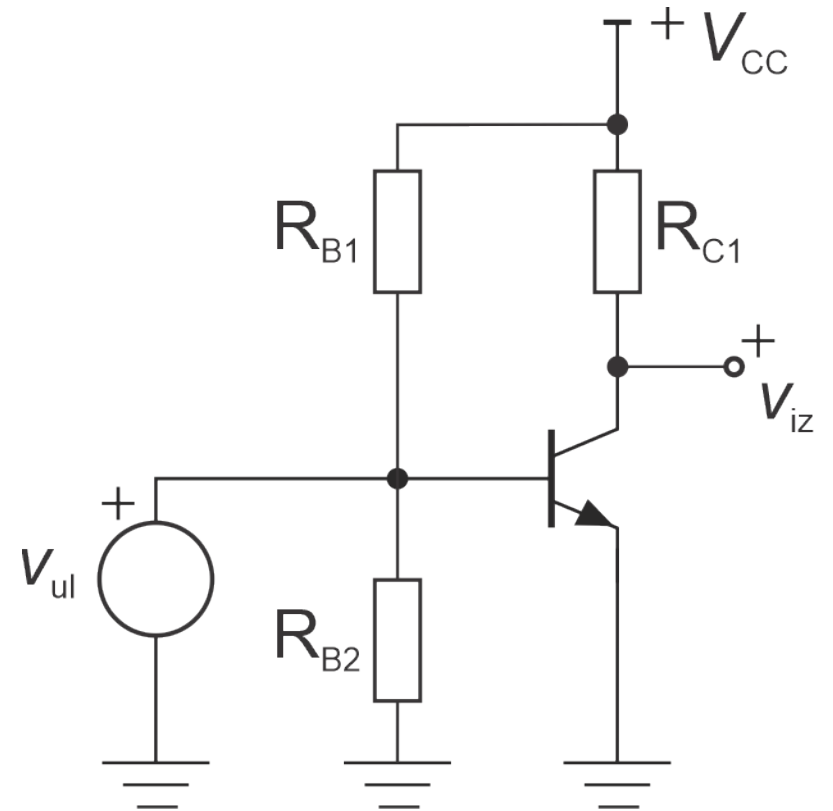
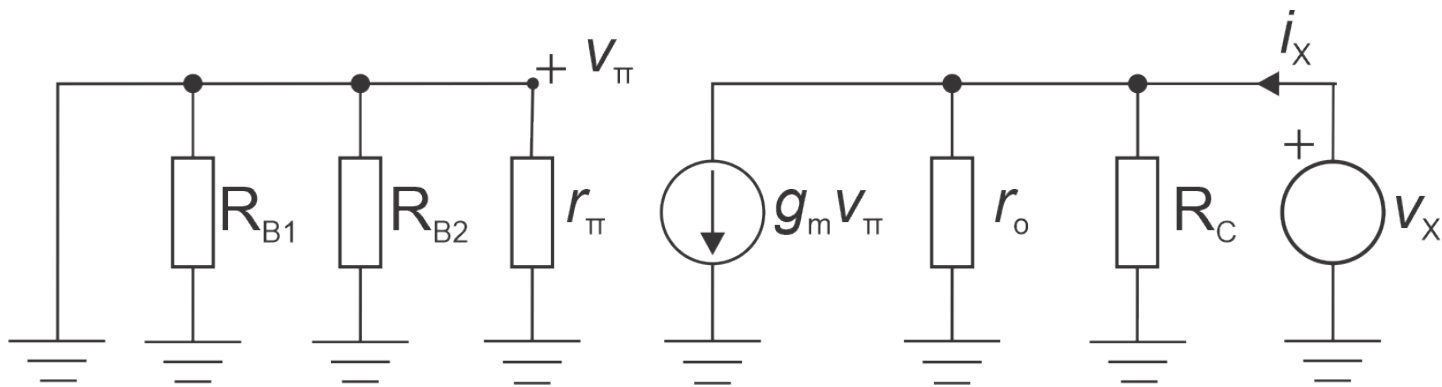
# Kola za polarizaciju

$$R_{ul} = R_{B1} \parallel R_{B2} \parallel r_{\pi}$$

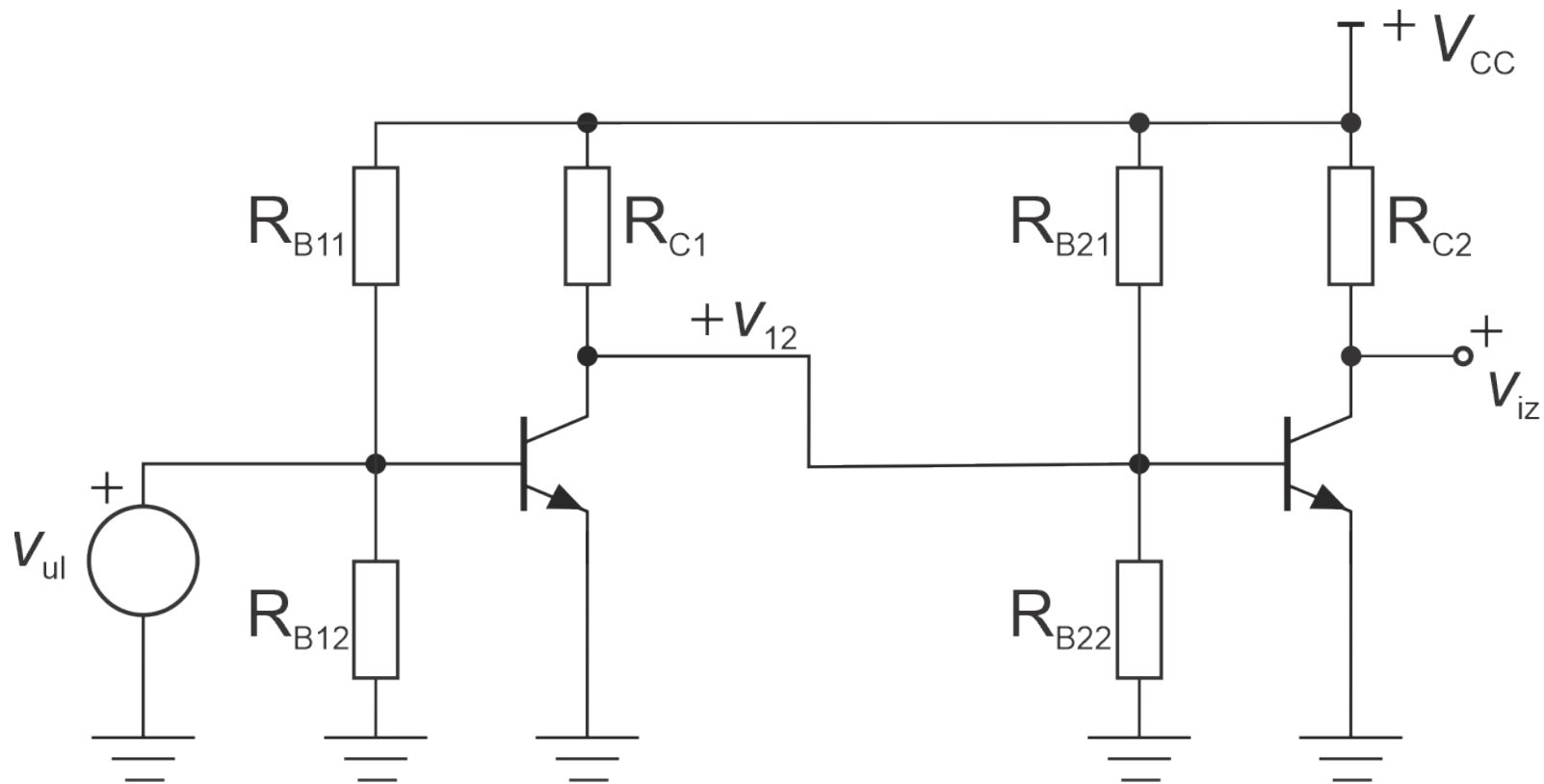


# Kola za polarizaciju

$$R_{iz} = r_o \parallel R_C$$

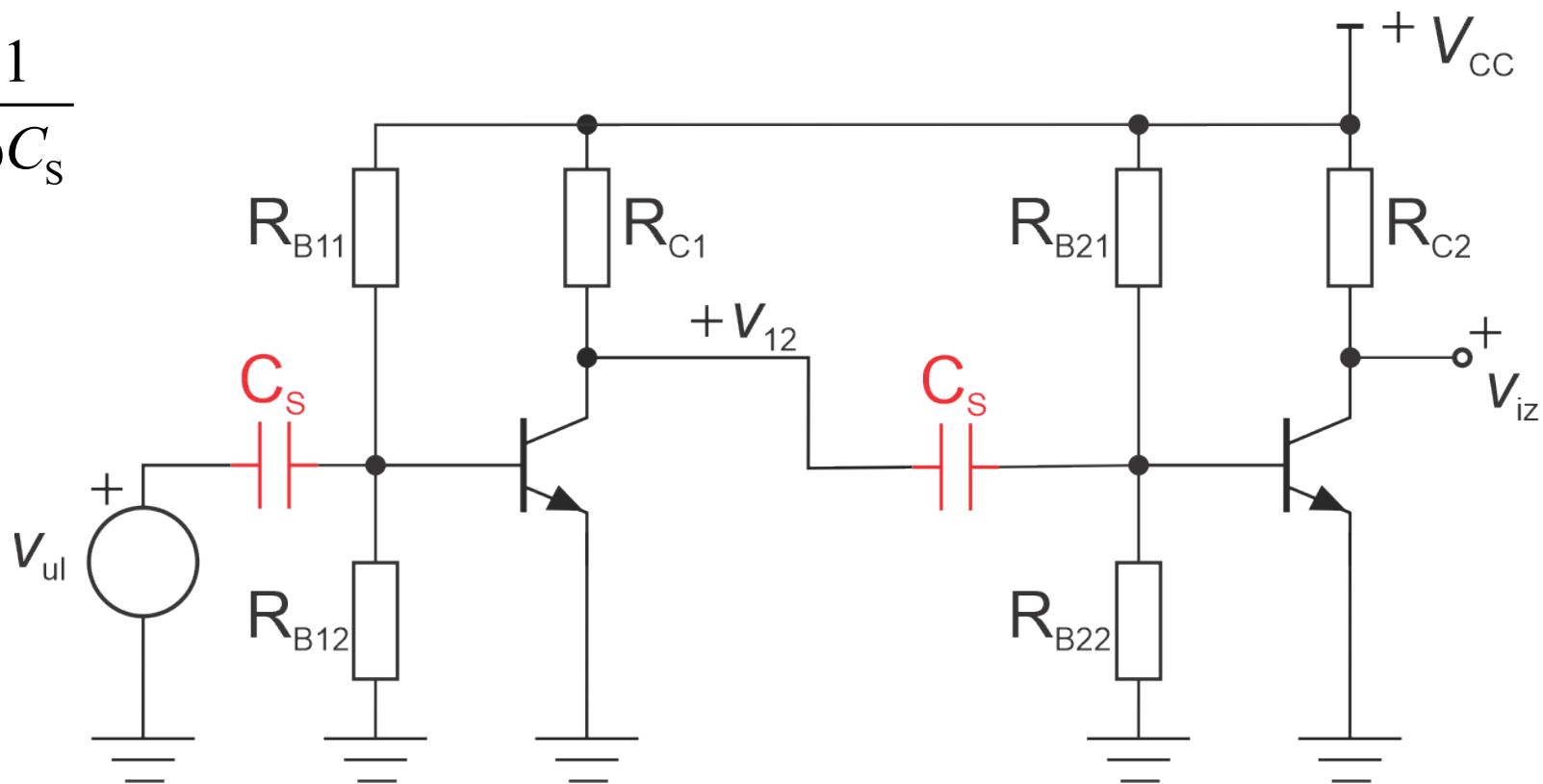


# Kola za polarizaciju



# Kola za polarizaciju

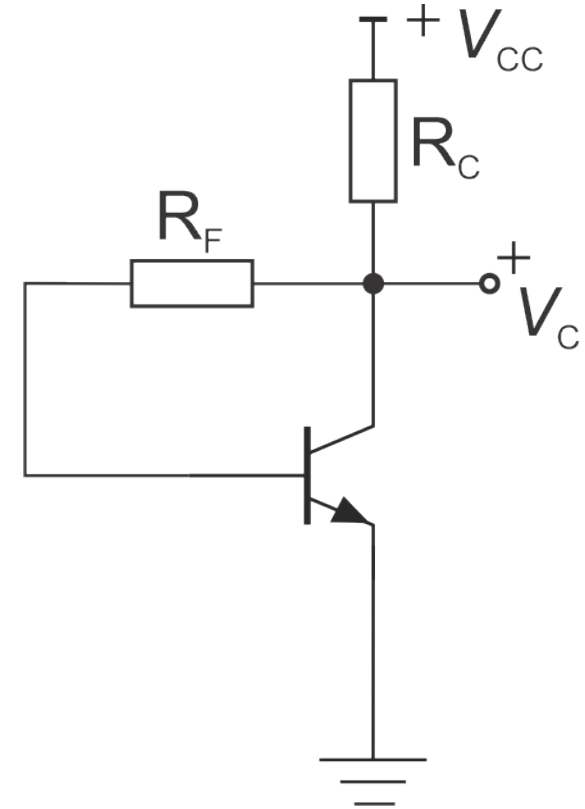
$$R_{ul2}, R_{ul2} \gg \frac{1}{\omega C_S}$$



# Kola za polarizaciju

- Self-bias kolo
- Mala osetljivost na promene  $V_{CC}$
- Tranzistor je uvek u aktivnom režimu:

$$V_B = V_C - I_B R_F$$



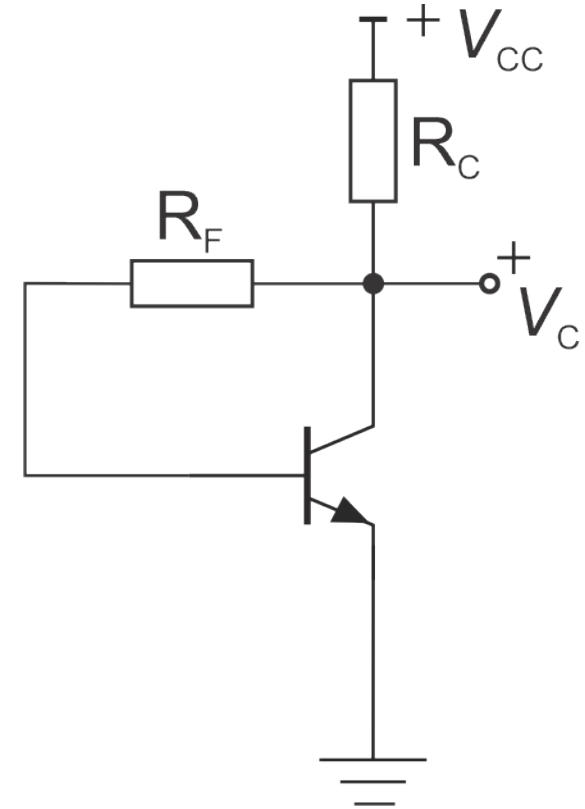
# Kola za polarizaciju

$$\beta \gg 1 \Rightarrow I_C \gg I_B$$

$$V_C = V_{CC} - I_C R_C$$

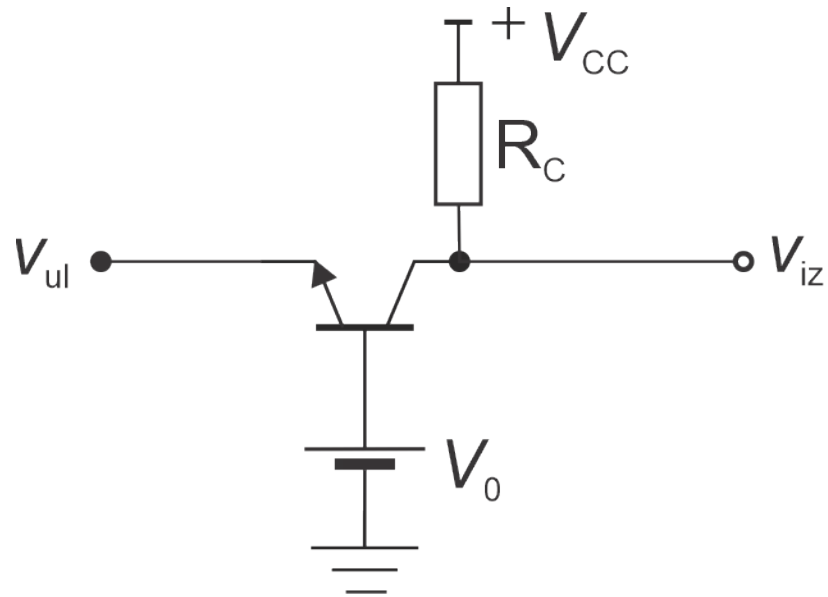
$$V_{BE} = V_{CC} - I_C R_C - I_B R_F$$

$$I_C = \frac{V_{CC} - V_{BE}}{R_C + R_F / \beta} \quad R_C \gg R_F / \beta$$



# Pojačavač sa zajedničkom bazom

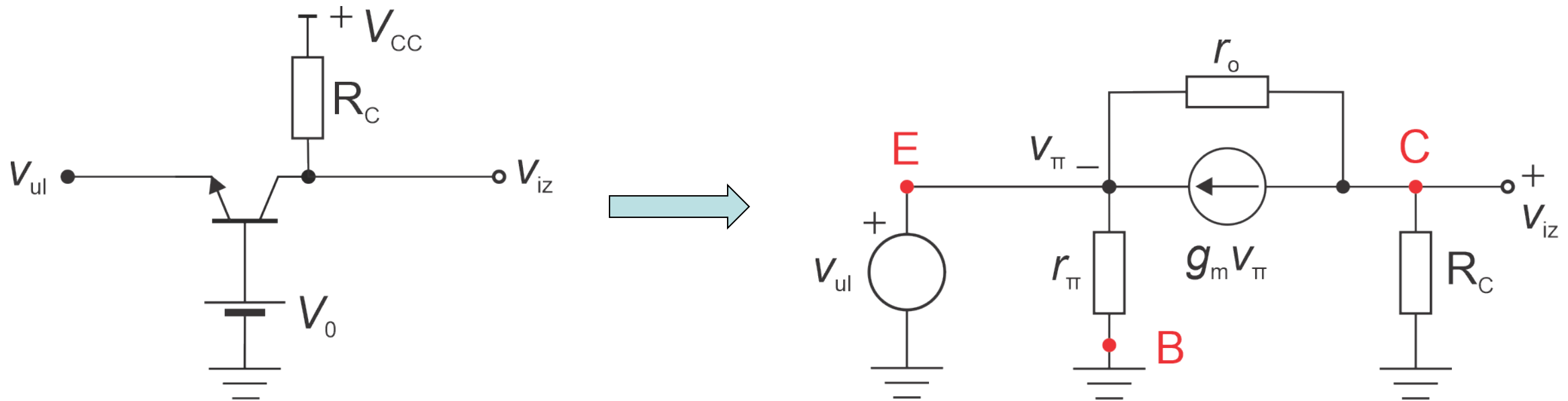
- Pojačanje, ulazna i izlazna impedansa





# Pojačavač sa zajedničkom bazom

- Kolo za male signale



# Pojačavač sa zajedničkom bazom – pojačanje

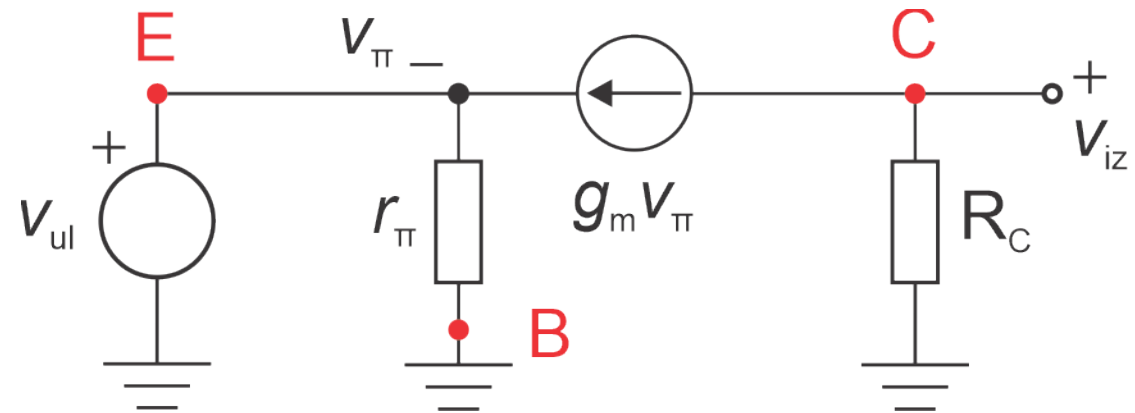
- Kolo za male signale, zanemarujemo Erlijev efekat ( $r_o = \infty$ )

$$v_{\pi} = -v_{ul}$$

$$v_{iz} = -g_m v_{\pi} R_C$$

$$v_{iz} = g_m R_C v_{ul}$$

$$A = g_m R_C$$



# Pojačavač sa zajedničkom bazom – ul. impedansa

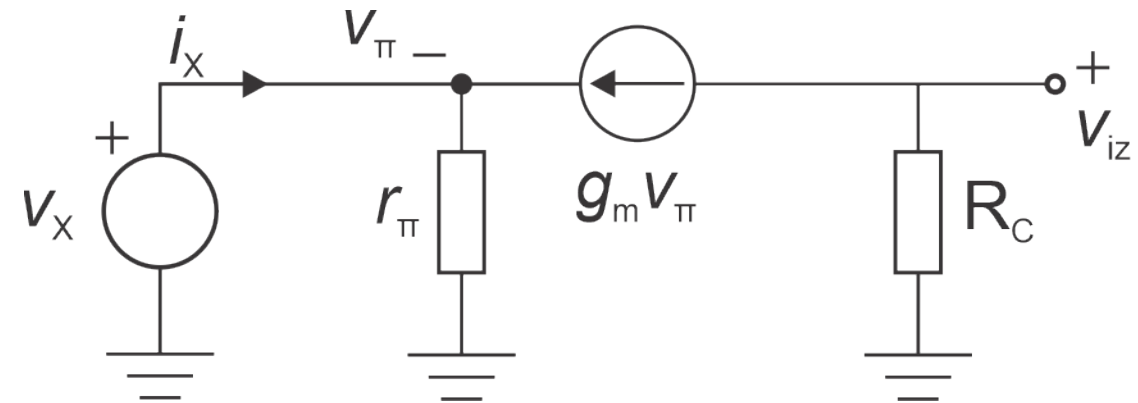
- Kolo za male signale, zanemarujemo Erlijev efekat ( $r_o = \infty$ )

$$-v_\pi = g_m v_\pi r_\pi + i_X r_\pi$$

$$-v_\pi (1 + g_m r_\pi) = i_X r_\pi$$

$$v_X (1 + \beta) = i_X r_\pi$$

$$R_{ul} = \frac{v_X}{i_X} = \frac{r_\pi}{1 + \beta} \approx \frac{1}{g_m}$$

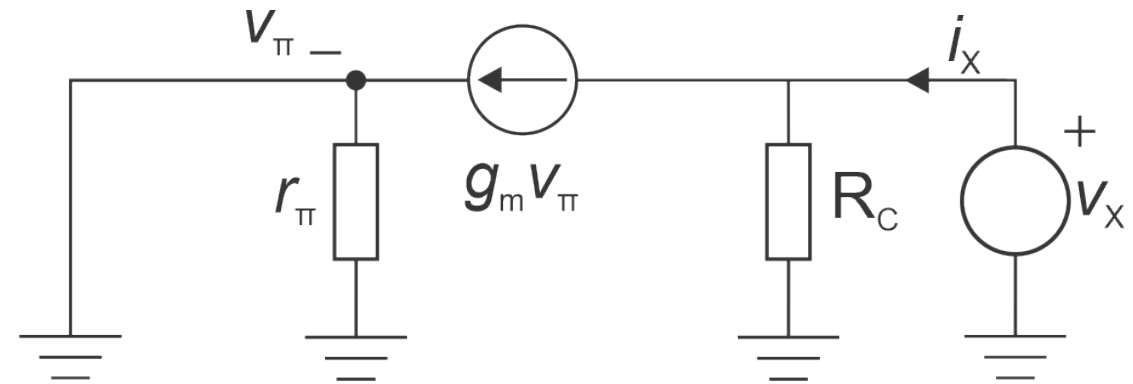


# Pojačavač sa zajedničkom bazom – iz. impedansa

- Kolo za male signale, zanemarujemo Erlijev efekat ( $r_o = \infty$ )

$$v_\pi = 0$$

$$R_{iz} = R_C$$



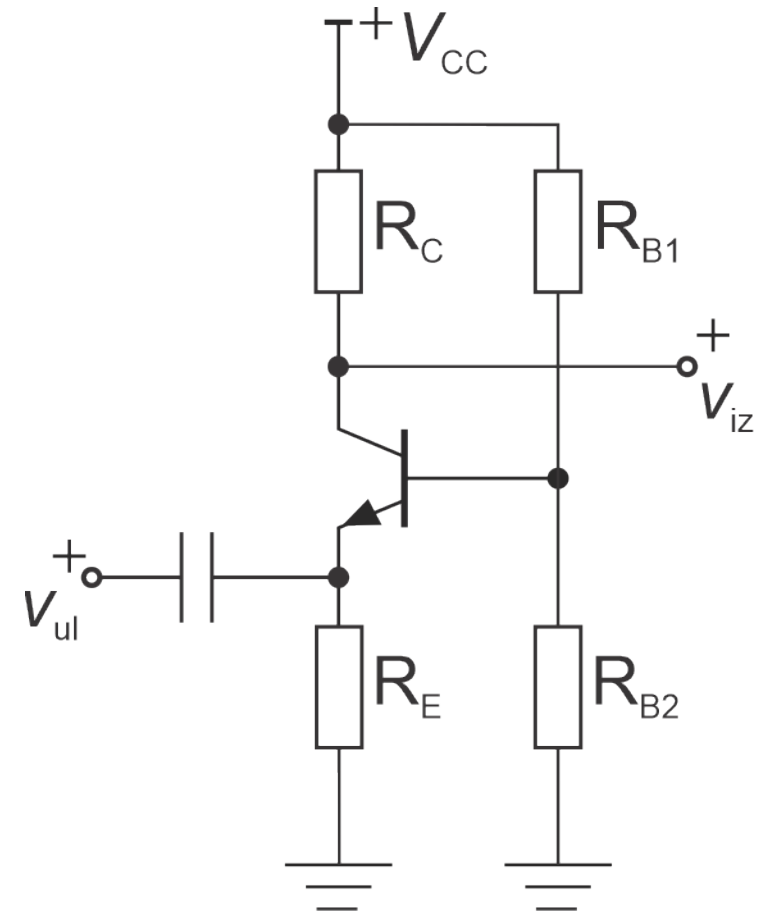
# Pojačavač sa zajedničkom bazom – polarizacija

$$R_E \gg 1/g_m$$

$$\frac{R_{B1}}{R_{B1} + R_{B2}} V_{CC} > I_C R_E + V_{BE}$$

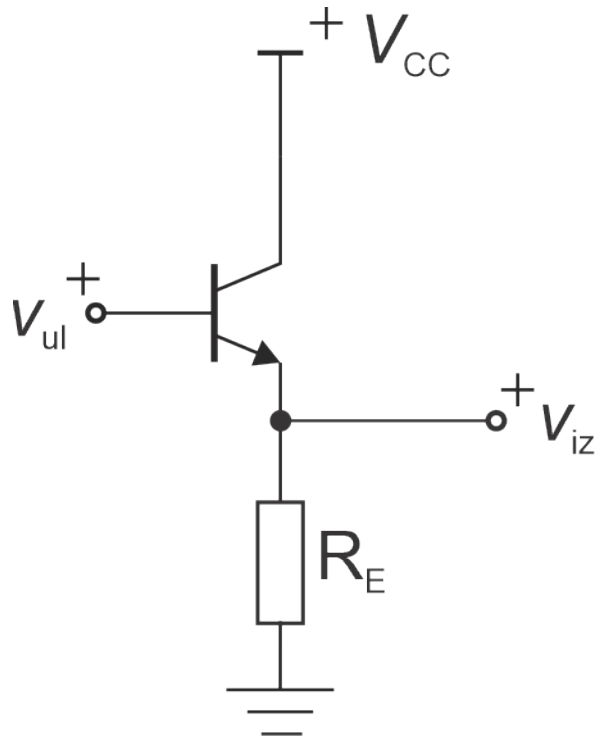
$$\frac{R_{B1}}{R_{B1} + R_{B2}} V_{CC} < V_{CC} - I_C R_C$$

$$R_{ul} = 1/g_m \parallel R_E$$



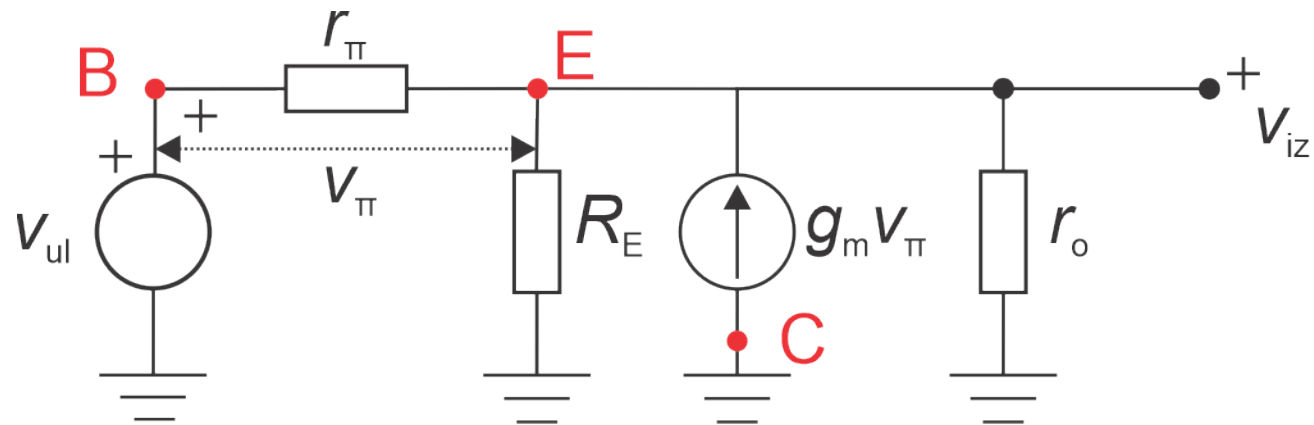
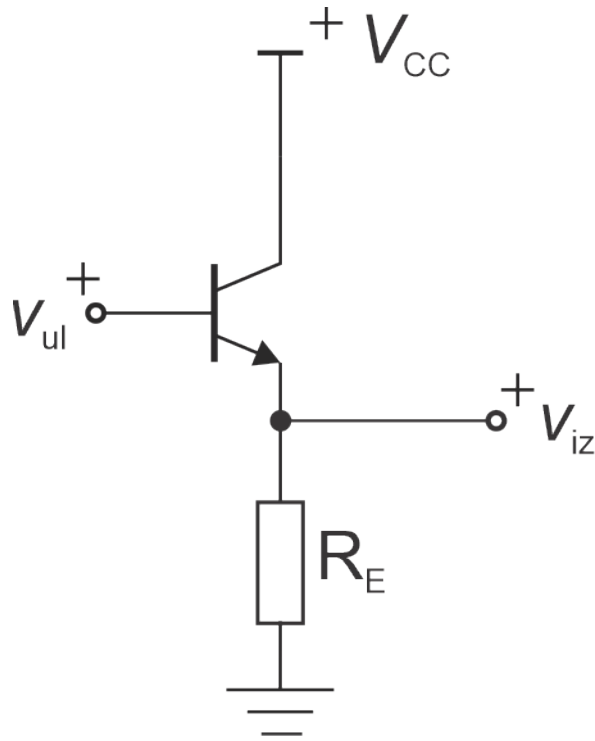
# Pojačavač sa zajedničkim kolektorom

- Pojačanje, ulazna i izlazna impedansa



# Pojačavač sa zajedničkim kolektorom

- Kolo za male signale



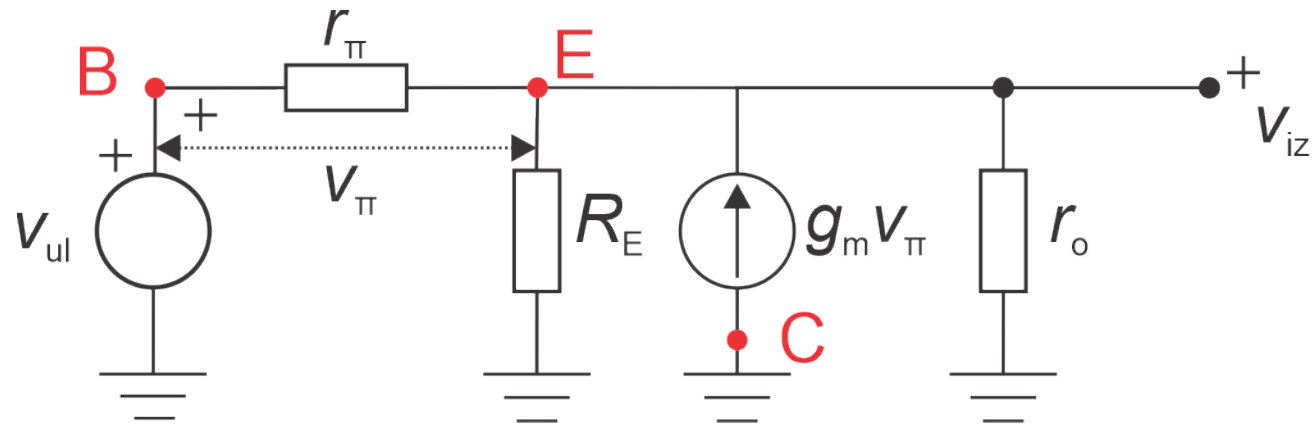
# Pojačavač sa zajedničkim kolektorom – pojačanje

$$i_E = \frac{v_{iz}}{R_E}, i_o = \frac{v_{iz}}{r_o}$$

$$\frac{v_\pi}{r_\pi} = \frac{v_{iz}}{R_E} - g_m v_\pi + \frac{v_{iz}}{r_o}$$

$$v_\pi = v_{ul} - v_{iz}$$

$$\frac{v_{ul} - v_{iz}}{r_\pi} = \frac{v_{iz}}{R_E} - g_m (v_{ul} - v_{iz}) + \frac{v_{iz}}{r_o}$$





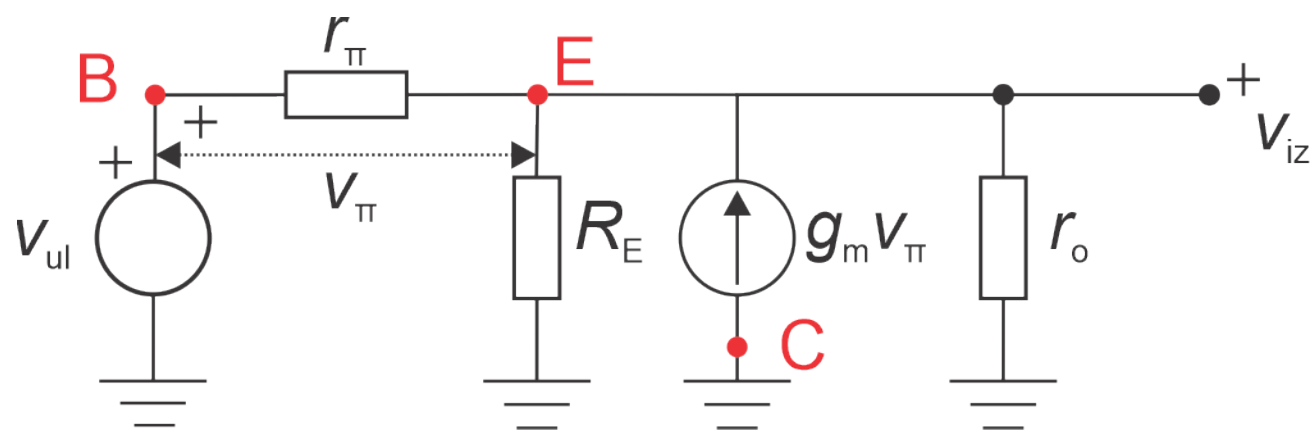
# Pojačavač sa zajedničkim kolektorom – pojačanje

$$\frac{v_{ul}}{r_{\pi}} + g_m v_{ul} = \frac{v_{iz}}{R_E} + \frac{v_{iz}}{r_o} + g_m v_{iz}$$

$$\frac{v_{iz}}{v_{ul}} = \frac{(R_E \parallel r_o)(1 + r_{\pi} g_m)}{r_{\pi} + g_m r_{\pi} (R_E \parallel r_o)} = \frac{(R_E \parallel r_o)(1 + \beta)}{r_{\pi} + \beta (R_E \parallel r_o)}$$

$$v_{ul} \left( \frac{1}{r_{\pi}} + g_m \right) = v_{iz} \left( \frac{1}{R_E} + \frac{1}{r_o} + g_m \right)$$

$$\frac{v_{iz}}{v_{ul}} = \frac{(1/r_{\pi} + g_m)}{(1/(R_E \parallel r_o) + g_m)}$$

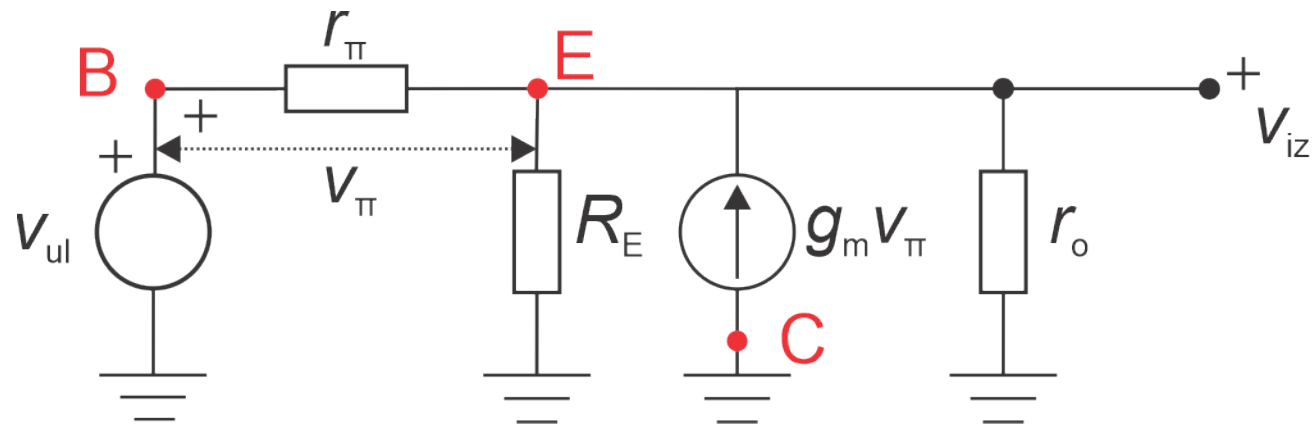


# Pojačavač sa zajedničkim kolektorom – pojačanje

$$A = \frac{(R_E \parallel r_o)(1 + \beta)}{r_\pi + \beta(R_E \parallel r_o)} \approx \frac{\beta(R_E \parallel r_o)}{r_\pi + \beta(R_E \parallel r_o)}$$

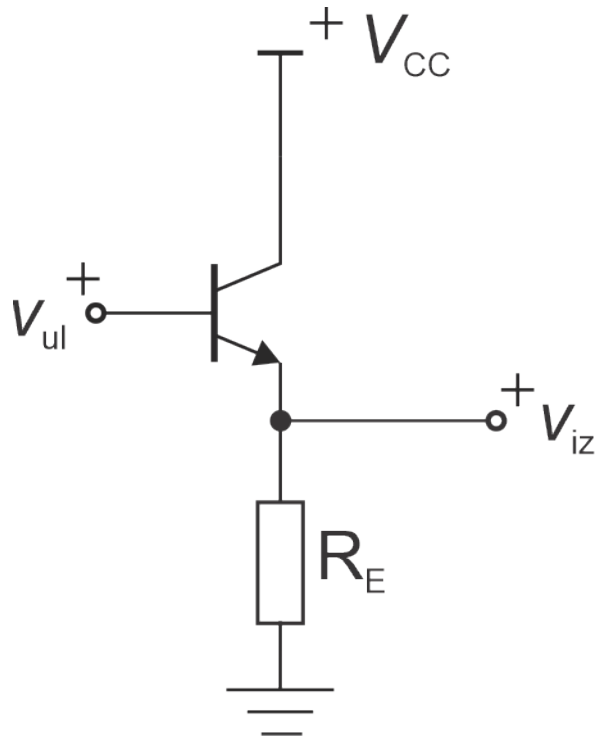
$$A \approx \frac{R_E \parallel r_o}{1/g_m + R_E \parallel r_o} < 1$$

$$A \approx \frac{R_E}{1/g_m + R_E}, \quad r_o = \infty$$



# Pojačavač sa zajedničkim kolektorom – ulazna imp.

- Kolo je ekvivalentno degenerisanom emitoru, za  $R_C=0$ .



$$R_{ul} = (\beta + 1)R_E + r_\pi$$

# Pojačavač sa zajedničkim kolektorom – izlazna imp.

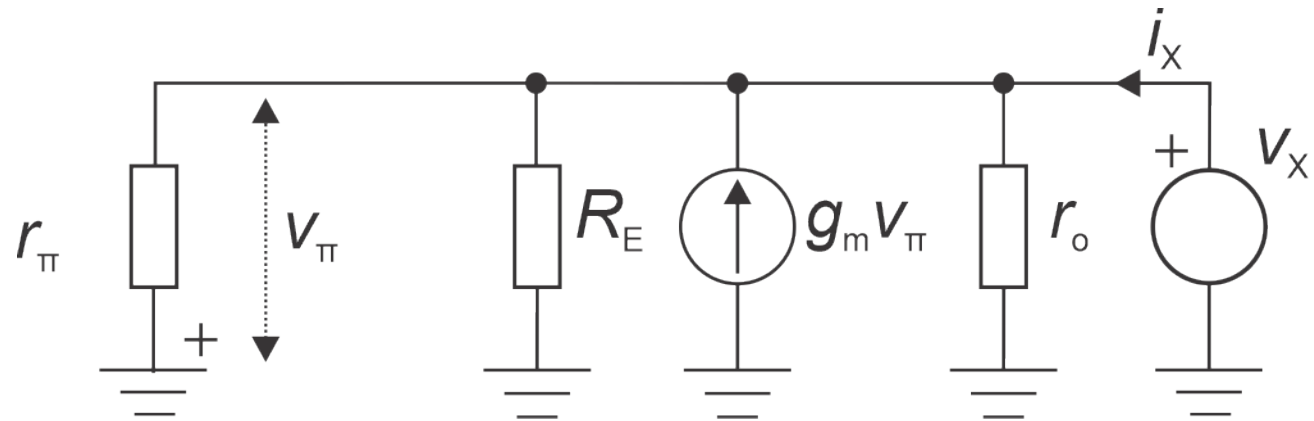
$$v_{\pi} = -v_X$$

$$i_X + g_m v_{\pi} = \frac{v_X}{r_{\pi}} + \frac{v_X}{R_E} + \frac{v_X}{r_o}$$

$$i_X = v_X \left( \frac{1}{r_{\pi}} + \frac{1}{R_E} + \frac{1}{r_o} + g_m \right)$$

$$R_{iz} = \frac{v_X}{i_X} = \frac{1}{\frac{1}{r_{\pi}} + \frac{1}{R_E} + \frac{1}{r_o} + g_m}$$

$$R_{iz} = \frac{v_X}{i_X} = r_{\pi} \parallel R_E \parallel r_o \parallel 1/g_m$$

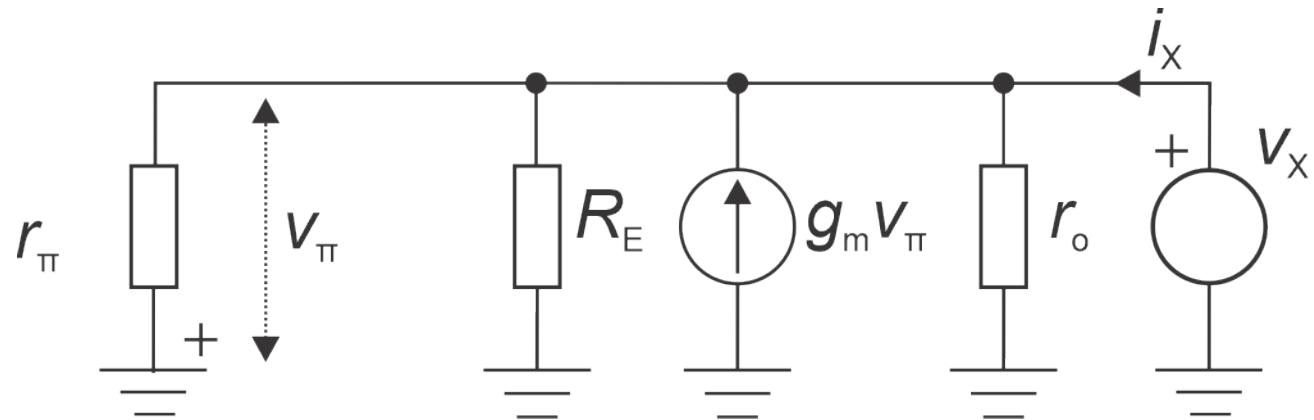


# Pojačavač sa zajedničkim kolektorom – izlazna imp.

- Pojednostavljen izraz,  $r_o = \infty$  i  $g_m = \beta/r_{\pi} \gg 1/r_{\pi}$

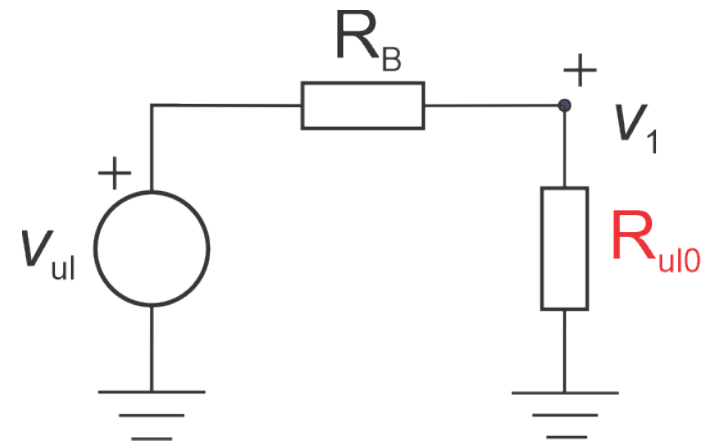
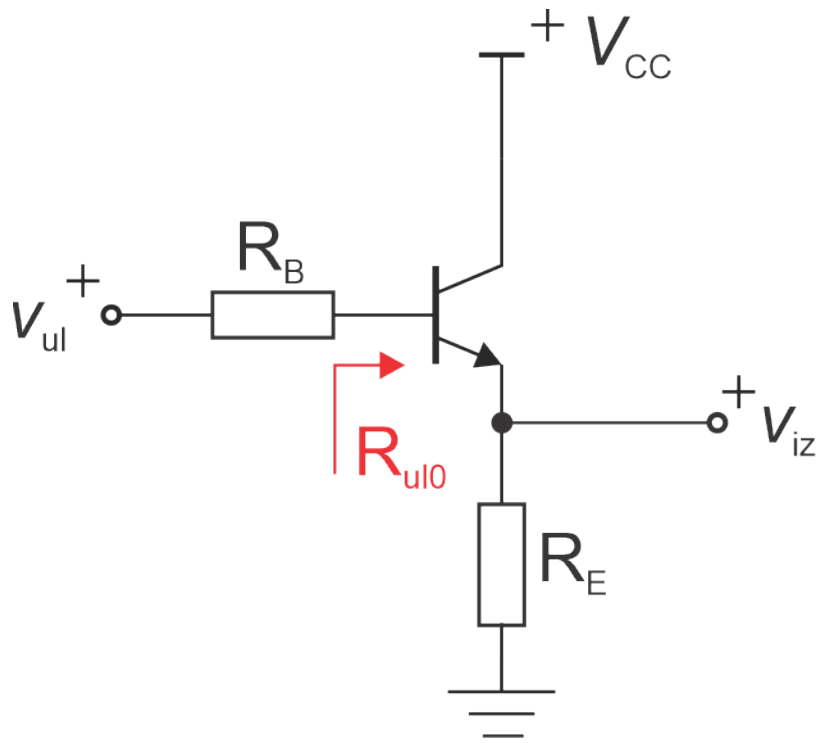
$$R_{iz} \approx \frac{1}{\frac{1}{R_E} + g_m}$$

$$R_{iz} \approx R_E \parallel 1/g_m$$



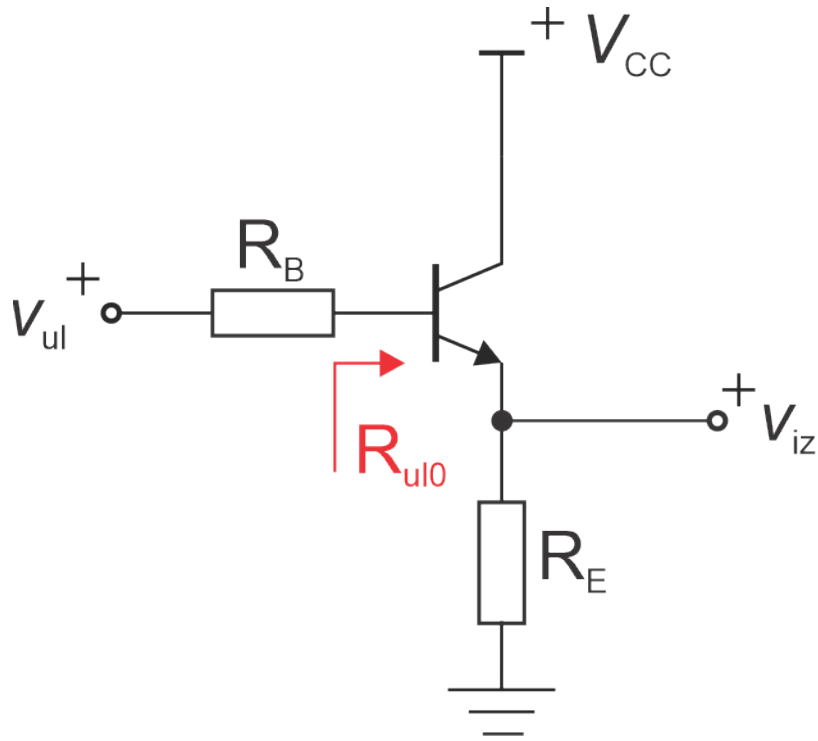
# Pojačavač sa zajedničkim kolektorom – polarizacija, $R_B$

- Otpornik u grani baze, pojačanje



$$V_1 = \frac{R_{ul}}{R_{ul} + R_B} V$$

# Pojačavač sa zajedničkim kolektorom – polarizacija, $R_B$



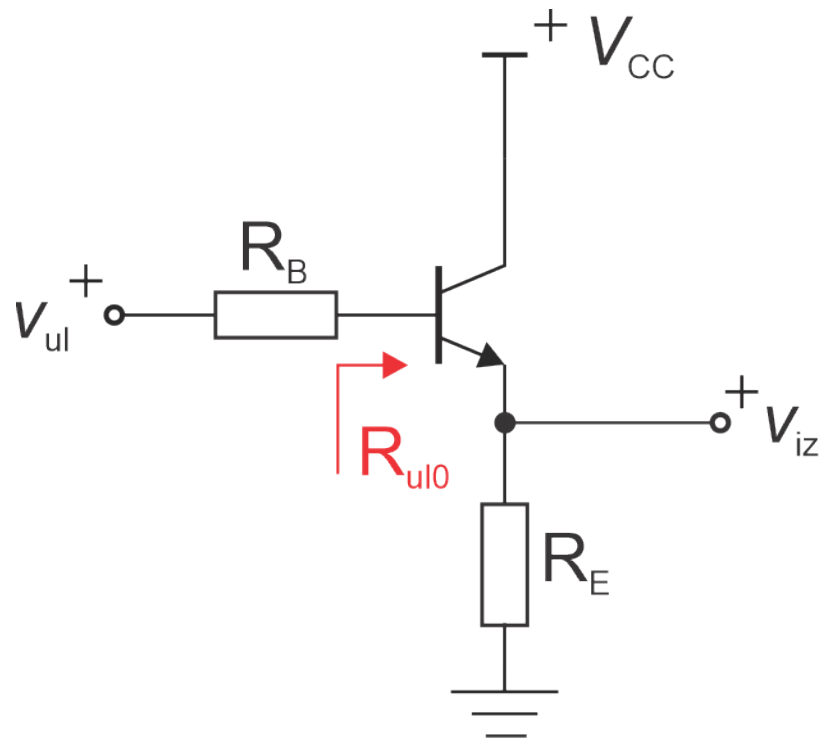
$$R_{ul0} = (\beta + 1)R_E + r_\pi$$

$$A_0 = \frac{R_E}{1/g_m + R_E}, \quad r_o = \infty$$

$$A = \frac{R_E}{1/g_m + R_E} \frac{R_{ul}}{R_{ul} + R_B}$$

$$A = \frac{R_E}{1/g_m + R_E} \frac{(\beta + 1)R_E + r_\pi}{(\beta + 1)R_E + r_\pi + R_B}$$

# Pojačavač sa zajedničkim kolektorom – polarizacija, $R_B$



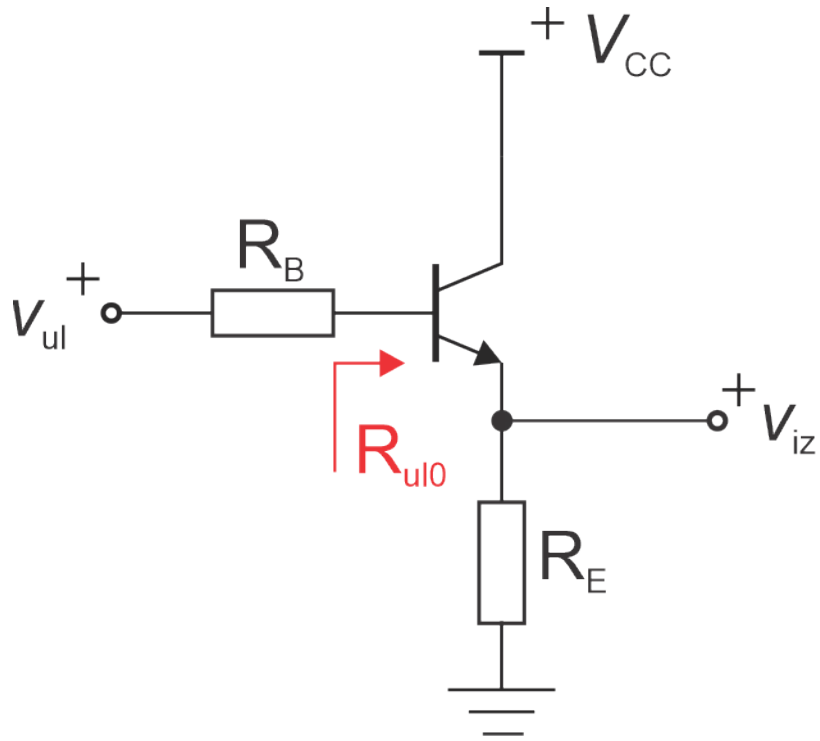
$$A = \frac{R_E}{1/g_m + R_E} \frac{R_E + \frac{r_\pi}{\beta + 1}}{R_E + \frac{r_\pi}{\beta + 1} + \frac{R_B}{\beta + 1}}$$

$$\frac{r_\pi}{\beta + 1} \approx \frac{r_\pi}{\beta} = \frac{1}{g_m}$$

$$A = \frac{R_E}{1/g_m + R_E} \frac{R_E + 1/g_m}{R_E + 1/g_m + \frac{R_B}{\beta + 1}}$$



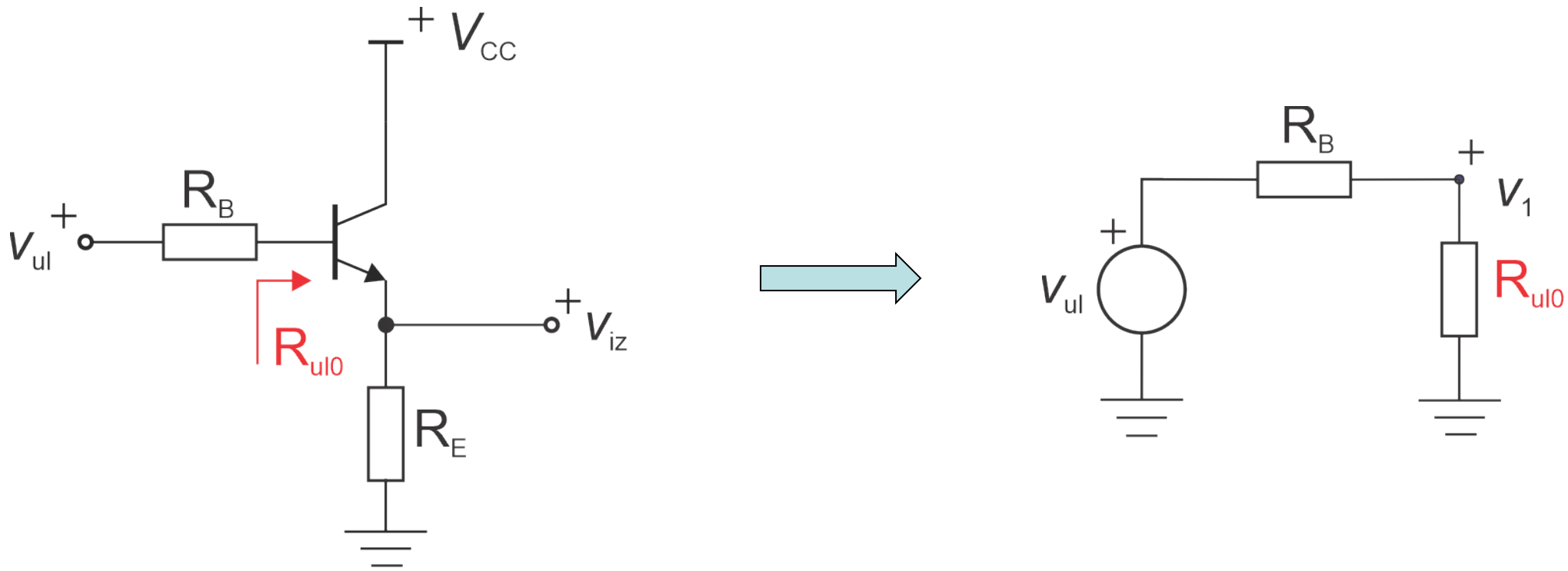
# Pojačavač sa zajedničkim kolektorom – polarizacija, $R_B$



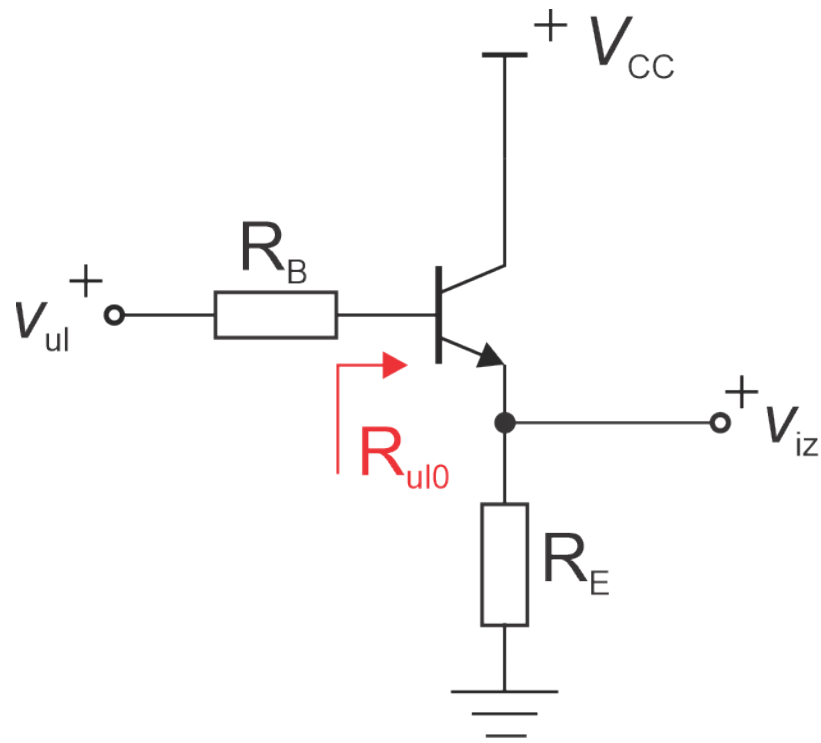
$$A = \frac{R_E}{R_E + 1/g_m + \frac{R_B}{\beta + 1}}$$

# Pojačavač sa zajedničkim kolektorom – polarizacija, $R_B$

- Otpornik u grani baze, ulazna impedansa



# Pojačavač sa zajedničkim kolektorom – polarizacija, $R_B$

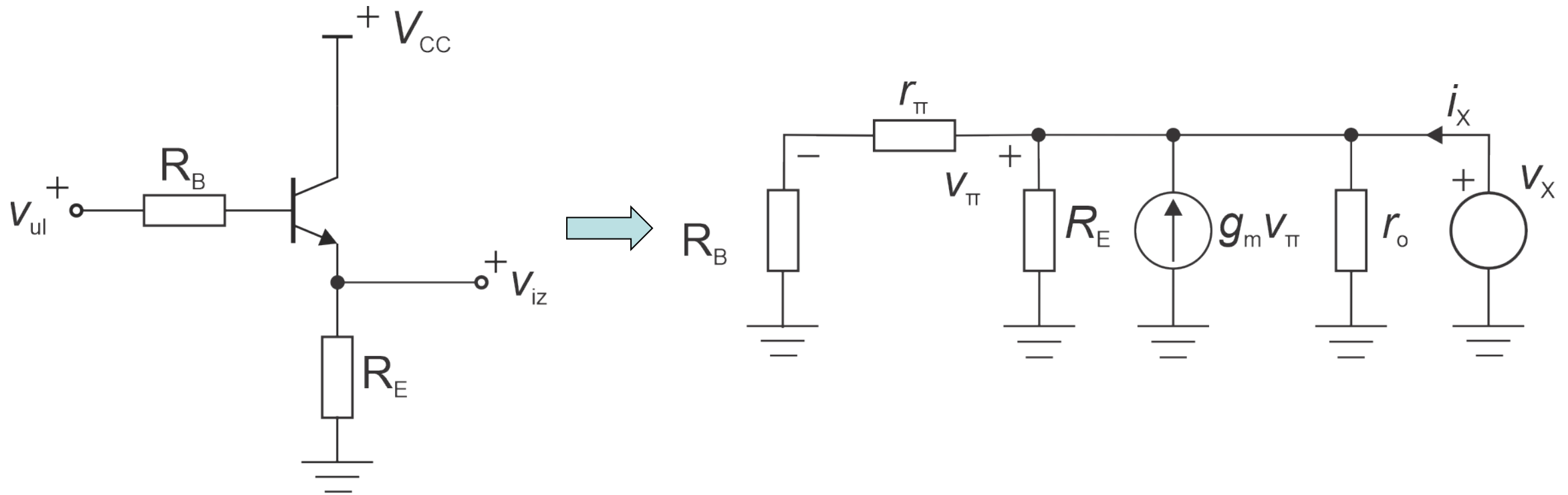


$$R_{ul0} = (\beta + 1)R_E + r_\pi$$

$$R_{ul} = (\beta + 1)R_E + r_\pi + R_B$$

# Pojačavač sa zajedničkim kolektorom – polarizacija, $R_B$

- Otpornik u grani baze, izlazna impedansa



# Pojačavač sa zajedničkim kolektorom – polarizacija, $R_B$

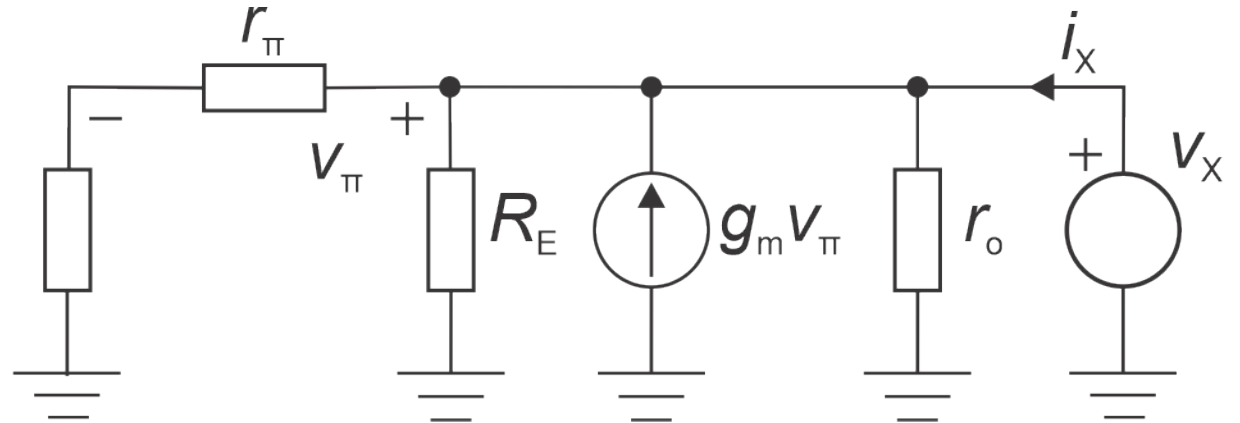
$$v_\pi = -\frac{r_\pi}{r_\pi + R_B} v_X$$

$$i_X + g_m v_\pi = \frac{v_X}{r_\pi + R_B} + \frac{v_X}{R_E} + \frac{v_X}{r_o}$$

$$i_X = v_X \left( \frac{1}{r_\pi + R_B} + \frac{1}{R_E} + \frac{1}{r_o} + \frac{g_m r_\pi}{r_\pi + R_B} \right) R_B$$

$$R_{iz} = \frac{v_X}{i_X} = \frac{1}{\frac{\beta + 1}{R_E + r_\pi} + \frac{1}{R_E} + \frac{1}{r_o}}$$

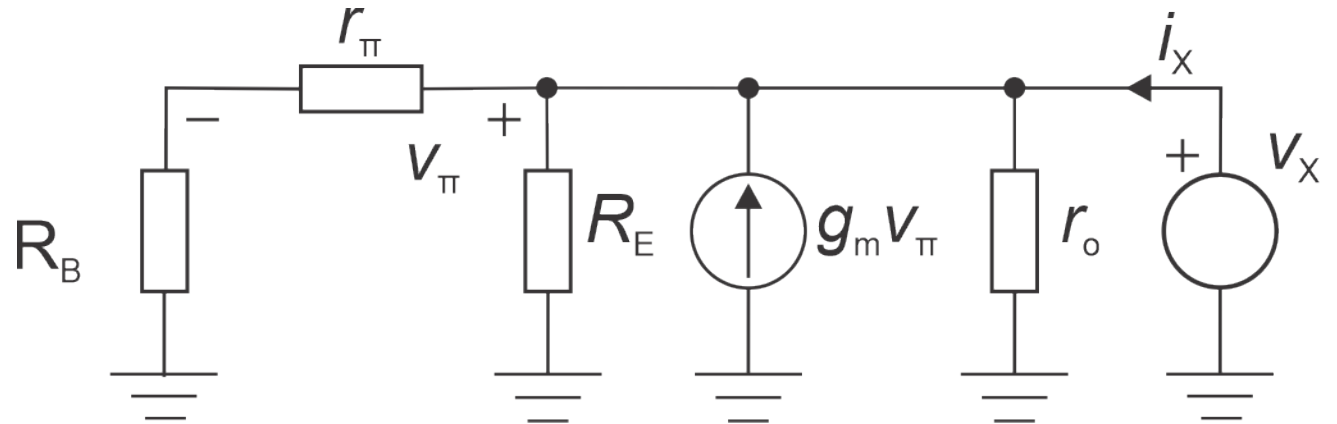
$$R_{iz} = \frac{v_X}{i_X} = \frac{R_B + r_\pi}{\beta + 1} \parallel R_E \parallel r_o$$



# Pojačavač sa zajedničkim kolektorom – polarizacija, $R_B$

- Pojednostavljen izraz,  $r_o = \infty$  i  $r_{\pi}/(\beta+1) \approx r_{\pi}/\beta = 1/g_m$

$$R_{iz} \approx R_E \parallel \left( 1/g_m + R_B/(\beta + 1) \right)$$



# Poređenje topologija pojačavača sa bipolarnim t.

Topologija	Naponsko pojačanje $A$	Fazni pomeraj	Ulazna impedansa $R_{ul}$	Izlazna impedansa $R_{iz}$
Zajednički emitor	$-g_m \cdot (R_C \parallel r_o)$	$\pi$	$r_\pi$	$r_o \parallel R_C$
Degenerisani emitor, $r_o = \infty$	$-\frac{g_m R_C}{1 + g_m R_E}$	$\pi$	$(\beta + 1)R_E + r_\pi$	$R_C$
Zajednički emitor sa naponskim razdelnikom	$-g_m \cdot (R_C \parallel r_o)$	$\pi$	$R_{B1} \parallel R_{B2} \parallel r_\pi$	$r_o \parallel R_C$
Zajednička baza, $r_o = \infty$	$g_m \cdot R_C$	0	$\frac{r_\pi}{1 + \beta} \approx \frac{1}{g_m}$	$R_C$
Zajednički kolektor	$\approx \frac{R_E \parallel r_o}{1/g_m + R_E \parallel r_o}$	0	$(\beta + 1)R_E + r_\pi$	$\approx R_E \parallel 1/g_m$